

Discussion of
**Incentive Constrained Risk Sharing,
Segmentation, and Asset Pricing**
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Question

- **What are asset pricing implications of collateral constraints?**
 - Simple, clean model with **endogenous constraints**

- **Results**
 - Assets trade at **discount** due to limited collateralizability
 - **Segmentation** of asset holdings by risk aversion
 - **Expected returns concave in β**

- **Novel features**
 - All assets **tradeable but limited collateralizability**
 - Heterogeneity in preferences

Outline

- **Model**
- **What is friction?**
 - Incentive compatibility, diversion, and borrowing constraint
 - Deriving collateral constraints from limited enforcement
- **Law of one price – does it hold or fail?**
 - Basis vs. discount and collateral premium
- **How general are results?**
 - Expected returns concave in β
 - Segmentation

Model

■ Simple and clean

- Static
 - Two dates 0 and 1
 - Consumption only at date 1
 - States $\omega \in \Omega$
- Pure exchange economy (no production)
- **“Canonical GE model”**

■ Motive for trade

- **Heterogenous preferences**
 - Mostly 2 types with CRRA $0 \leq \gamma_1 \leq \gamma_2 \leq 1$
- Initial endowments share of aggregate endowment at date 1

■ Assets

- Tradeable trees (or “assets”) pay non-negative dividends $d_j(\omega) \geq 0$
- Limited collateralizability (or pledgeability) (see below)

What is Friction?

- **Incentive compatibility constraint** – “imperfect recoverability”
 - Agent “can make a take-it-or-leave-it offer to ... creditors”
 - Creditors “can only seize fraction $1 - \delta \in (0, 1]$ of ... assets”
 - See Kiyotaki/Moore (1997)’s motivation for collateral constraint

- **Notation** – **collateralizability** θ , where $\theta \equiv 1 - \delta$; Kiyotaki (1998)

- Alternative motivation: **Diversion** – agents “can divert” $1 - \theta$
 - As in Bolton/Scharfstein (1990), Holmström/Tirole (1997), DeMarzo/Fishman (2007), DeMarzo/Sannikov (2006)

What is Friction? (Cont'd)

■ Strategic default

- Agent who strategically defaults “obtains fraction $1 - \theta$ of his *long* positions in trees and Arrow securities,” so

$$\hat{c} = (1 - \theta) \left[\int d_j dN_j + a^+ \right]$$

where dependence of agent's type i and state ω is suppressed

■ Incentive compatibility constraint

$$c \geq \hat{c}$$

■ State-contingent borrowing constraint

- Using budget constraint and substituting into IC, we get

$$\theta \left[\int d_j dN_j + a^+ \right] \geq a^-$$

where a^- is short position with net position $a = a^+ - a^-$

- Weakly optimal to choose either $a^+ = 0$ or $a^- = 0$ (Lemma 1), so

$$\theta \int d_j dN_j \geq -a$$

What is Friction? – Limited Enforcement

- **Risk sharing and asset pricing with limited enforcement**
 - Kehoe/Levine (1993), Kocherlakota (1996), Alvarez/Jermann (2000)
 - Default with exclusion (autarky as outside option)
- **Limited enforcement without exclusion (1)**
 - Chien/Lustig (2010), Lustig/van Nieuwerburgh (2005)
 - Trees/houses perfectly collateralizable but not labor income
- **Limited enforcement without exclusion (2)**
 - Rampini/Viswanathan (2010, 2013, forthcoming, 2018)
 - **Imperfect collateralizability** of capital/houses but not cash flow
- **This paper: Only imperfectly collateralizable trees**

Deriving Collateral Constraints from Limited Enforcement

■ Derivation à la Rampini/Viswanathan

- **Limited enforcement (LE):** Agents can default on promises and abscond with $1 - \theta$ of any **trees** they hold

$$u(c) \geq u(\hat{c}) \quad (\text{LE})$$

where

$$\hat{c} \equiv (1 - \theta) \int d_j dN_j$$

■ Agent's problem

$$\max_{c, a, N_j} E[u(c)]$$

subject to (LE), $\forall \omega \in \Omega$, and

$$w \geq \sum_{\omega \in \Omega} q(\omega) a(\omega) + \int p_j dN_j$$

$$a + \int d_j dN_j \geq c, \quad \forall \omega \in \Omega$$

Collateral Constraints Derived à la Rampini/Viswanathan

■ Limited enforcement (LE) \Leftrightarrow Collateral constraints (CC)

- Budget constraint next period binds so write (LE) as

$$u\left(a + \int d_j dN_j\right) \geq u\left((1 - \theta) \int d_j dN_j\right)$$

- Since $u(c)$ is strictly increasing, write equivalently

$$a + \int d_j dN_j \geq (1 - \theta) \int d_j dN_j$$

and rearrange to get **collateral constraint (CC)**

$$\theta \int d_j dN_j \geq -a \tag{CC}$$

- Directly determines net promise ($a = a^+ - a^-$)

- Long positions in collateralized claims fully collateralizable so

$$\theta \int d_j dN_j + a^+ \geq a^-$$

- θ does not multiply a^+ – Lemma 1 not required
- Timing: first, agents' default decisions; then payments implemented

Alternative Implementation with Short Sale Constraints

■ Implementation: fully levered trees and short sale constraints

- “Hedging implementation” in Rampini/Viswanathan
- Suppose lever all trees fully $-\hat{a} \equiv \theta \int d_j dN_j$
- Then buy back collateralized claims (if necessary) $h \equiv a - \hat{a}$
- Rewrite collateral constraint as **short sale constraint (SSC)**

$$a + \theta \int d_j dN_j = a - \hat{a} = h \geq 0 \quad (\text{SSC})$$

■ Agent's problem

$$\max_{c, h, N_j} E[u(c)]$$

subject to (SSC), $\forall \omega \in \Omega$, and

$$w \geq \sum_{\omega \in \Omega} q(\omega) h(\omega) + \int \wp_j dN_j$$

$$h + (1 - \theta) \int d_j dN_j \geq c, \quad \forall \omega \in \Omega$$

where **down payment** $\wp_j \equiv p_j - \theta \sum_{\omega \in \Omega} q(\omega) d_j(\omega)$

Law of One Price – Does it Hold or Fail?

■ Law of One Price does not hold due to basis

- Define $M(\omega) \equiv \frac{q(\omega)}{\pi(\omega)}$ and $A_i(\omega) \equiv \frac{\mu_i(\omega)}{\lambda_i \pi(\omega)}$ then

$$p_j \geq \mathbb{E}[Md_j] - (1 - \theta)\mathbb{E}[A_i d_j]$$

so basis relative to replicating portfolio

■ Two pricing kernels! (One agent-specific)

- Pricing kernel for collateralized claims $M(\omega)$
- Pricing kernel for non-collateralizable part $M_i(\omega)$

$$M_i(\omega) \equiv \frac{u'_i(c(\omega))}{\lambda_i} = \frac{q(\omega)}{\pi(\omega)} - \frac{\mu_i(\omega)}{\lambda_i \pi(\omega)}$$

and therefore

$$p_j \geq \theta \mathbb{E}[Md_j] + (1 - \theta)\mathbb{E}[M_i d_j]$$

- Collateralized claims premium (non-collateralizable part discount)

$$M(\omega) \geq M_i(\omega)$$

- Here: non-collateralizable part still tradeable – clever

How General are Results?

■ Results for 2-by-2 case: 2 agent types and 2 states

- Asset structure

$$d_j(\omega) = (1 - j)\mathbf{1}(\omega_1) + j\mathbf{1}(\omega_2)$$

where ω_2 is high aggregate endowment state

■ **Segmentation** – do not hold market portfolio!

- Less (more) risk averse hold high (low) consumption beta assets
- Intuition seems general – can we say more?
- Would intermediate type hold intermediate assets or all assets?
- First best with heterogeneity in risk aversion similar (Dumas (1989))?

■ **Concavity** in consumption beta (Black (1972))

- Less (more) risk averse discounts low (high) state more

$$M_1(\omega_1) < M(\omega_1) \quad \text{and} \quad M_2(\omega_2) < M(\omega_2)$$

- Intermediate assets have higher returns – general?

Conclusion

■ Clever model

- **Limited collateralizability of perfectly tradeable assets**
- No idiosyncratic risk instead heterogeneity in risk aversion
- Interesting implications – segmentation and concave expected returns

■ Suggestions

- Friction? – Embrace **limited enforcement**
 - Derive collateral constraints à la Rampini/Viswanathan
 - Diversion is a diversion
- Generality?
- Dynamics?