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# The Low Rate Environment and the Fragility of Market Risk Insurance

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# Liabilities of U.S. financial institutions in 2019.Q2

Liability	Trillion \$
Mutual funds	16.7
	10.7
Savings deposits	
Life insurance	7.5
Private DC plans	6.9
Private DB plans	3.5

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- Most of the insurance literature about demand side.
  - ► Yaari (1965) and Rothschild and Stiglitz (1976).
- Less work on supply-side frictions.
  - Financial/regulatory frictions (corporate finance) and market power (IO).

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# Composition of life insurance liabilities in 2015

Liability	Trillion \$
Variable annuities (separate accounts)	1.8
Life insurance	1.5
Traditional annuities	1.0
Pension fund liabilities	0.7
Other reserves (accident & health)	0.3

Risk-sharing functions of life insurers:

- 1. Diversify idiosyncratic risk: Traditional life/health products.
- 2. Market risk insurance: Reallocate aggregate risk across
  - ► Investors with heterogeneous risk preferences (Dumas 1989).
  - Generations, taking on the traditional role of pension plans and Social Security (Allen and Gale 1997).

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The changing risk exposures in the life insurance sector

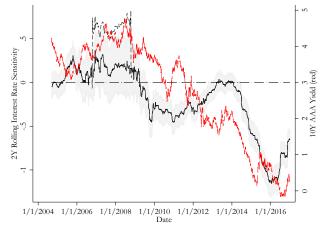
$$r_{\textit{Insurance},t}^{e} = \alpha + \beta_{m} r_{mt}^{e} - \rho_{y} 10 \Delta y_{t}^{(10)} + \epsilon_{t}.$$

Sample	'00-'07	'10-'18	'00-'07	'10-'18	'15-'18
$\beta_m$	0.60	1.43	0.54	1.17	1.00
	(4.90)	(15.95)	(4.21)	(12.84)	(7.13)
$ ho_y$			-0.27	-0.81	-1.09
			(1.33)	(5.48)	(4.90)
$\alpha$ (%)	0.21	-0.55	0.28	-0.15	-0.37
	(0.42)	(-1.65)	(0.56)	(-0.49)	(-0.92)
Т	96	99	96	99	39
$R^2$	0.203	0.724	0.218	0.790	0.781

- 1. CAPM: The market beta increased and the alpha declined since the financial crisis.
- 2. The equity of life insurers is becoming increasingly sensitive to changes in long-term interest rates.

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Interest rate exposure of life insurers in the EU



 Magnitude similar as in the US: a 1% decline in 10-year rates corresponds to a 10% decline in insurers' equity prices.

Based on Barbu, Koijen, and Yogo (in progress).

Questions		

1. What do life insurers insure?

- Market risk through minimum return guarantees.
- Variable annuity = Mutual fund + Long-dated put option
- ▶ \$1.5 trillion or 34% of U.S. life insurer liabilities in 2015.

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Questions					

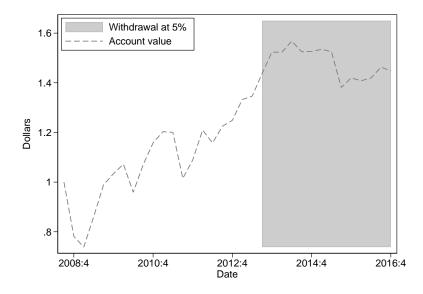
- 1. What do life insurers insure?
  - Market risk through minimum return guarantees.
  - Variable annuity = Mutual fund + Long-dated put option
  - ▶ \$1.5 trillion or 34% of U.S. life insurer liabilities in 2015.
- 2. How do they insure market risk?
  - Financial frictions and market power interact with aggregate shocks.
  - After the 2008 financial crisis,
    - Pricing: Fees increased and sales fell.
    - Contract characteristics: Insurers made guarantees less generous or exited to limit risk exposure.
    - Moved liabilities off balance sheet through reinsurance.

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Example:	MetLife Se	ries VA			

- ► Sold by MetLife Insurance Company USA.
- American Funds Growth Allocation Portfolio: Mutual fund with a target equity allocation of 70–85%.
- ► Annual base contract expense of 1.3%.
- Guaranteed Lifetime Withdrawal Benefit: Optional minimum return guarantee with
  - Annual fee of 0.5%.
  - Rollup rate (guaranteed return) of 5%.
  - Withdrawal rate of 5%.

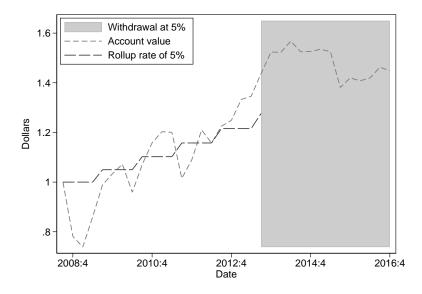
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# Example of a guaranteed living withdrawal benefit



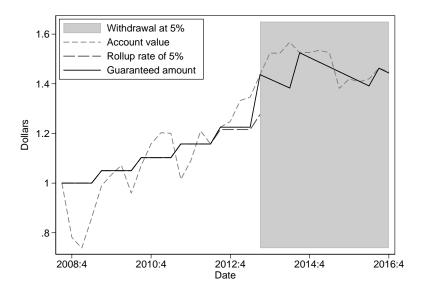
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# Example of a guaranteed living withdrawal benefit



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# Example of a guaranteed living withdrawal benefit



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# How are variable annuities regulated?

 Insurance regulators and rating agencies use the risk-based capital ratio:

$$\mathsf{RBC} = \frac{\mathsf{Assets} - \mathsf{Reserves}}{\mathsf{Required capital}}$$

- The value of VA guarantee (put option) increases with lower stock prices, lower interest rates, and higher volatility.
  - 1. Reserves increase because of revaluation.
  - 2. Required capital increases through risk exposure.
- An empirical measure of the value of VA guarantees:

Reserve valuation 
$$= \frac{\mathsf{Reserves}}{\mathsf{Account}}$$
 value

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#### Data on the variable annuity market

- Morningstar (1999:1–2015:4):
  - ► Quarterly contract-level data on sales, fees, and characteristics.
- ▶ NAIC General Interrogatories Part 2 Table 9.2 (2005–2015):
  - Annual data on VA account value, reserve value, and amount of reserves reinsured.
- A.M. Best Company (2005–2015):
  - Annual financial statements.
  - A.M. Best rating.

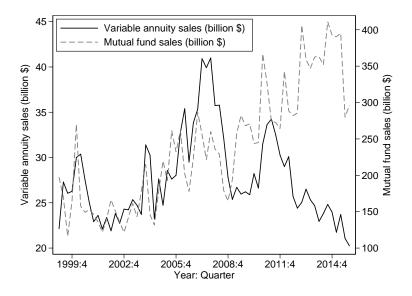
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# Summary statistics for the variable annuity market

	VA lia	bilities		
		Percent	Number	Reserve
		of total	of	valuation
Year	Billion \$	liabilities	insurers	(percent)
2005	1,071	35	45	0.9
2006	1,276	38	47	0.8
2007	1,435	41	46	0.8
2008	1,068	34	44	4.1
2009	1,195	35	43	3.4
2010	1,344	36	43	2.5
2011	1,358	35	42	4.9
2012	1,434	36	39	3.9
2013	1,606	37	40	1.8
2014	1,599	37	38	2.3
2015	1,499	35	38	2.9

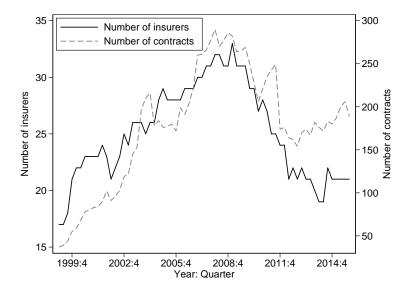
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# Variable annuity sales



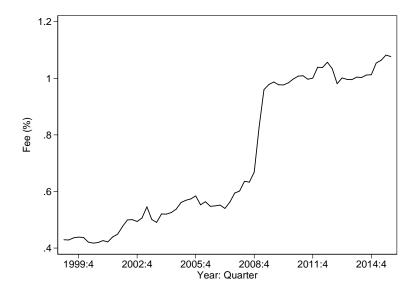
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#### Number of insurers and contracts offering VA guarantees



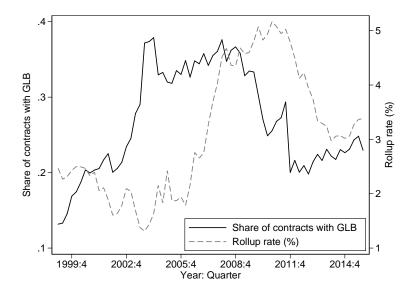
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# Fees on variable annuity guarantees



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#### Rollup rates on variable annuity guarantees



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# Evidence for supply-side fragility

- Fees increased and sales fell.
- Changing contract characteristics: Insurers made guarantees less generous to limit risk exposure.
  - Lower rollup rates (intensive margin).
  - Exit the market for guarantees (extensive margin).

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- Supply-side hypotheses:
  - 1. Updating of priors regarding tail risk (e.g., high market volatility or prolonged period of low interest rates).
  - 2. Higher valuation of existing liabilities lowers risk-based capital.

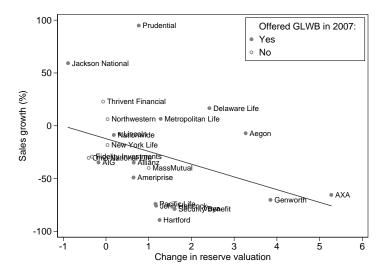
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- Supply-side hypotheses:
  - 1. Updating of priors regarding tail risk (e.g., high market volatility or prolonged period of low interest rates).
  - 2. Higher valuation of existing liabilities lowers risk-based capital.
- In the cross section, insurers that experienced larger increases in reserve valuation should
  - 1. Reduce sales more.
  - 2. Move liabilities off balance sheet through reinsurance.

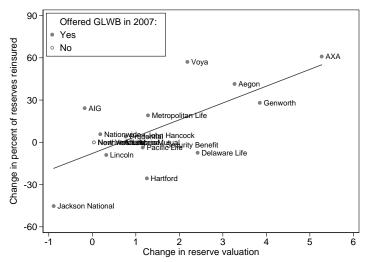
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#### Sales growth versus change in reserve valuation



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# Change in percent of reserves reinsured versus change in reserve valuation



Introduction	Background	Data	Model	Estimation	Conclusion

# A model of variable annuity supply

- Key frictions:
  - 1. Financial frictions: Issuance of new contracts increases required capital.
  - 2. Market power: Insurers compete by Bertrand pricing in an oligopolistic market.
- ► In response to an adverse shock to risk-based capital, insurer
  - 1. Increases prices.
  - 2. Changes contract characteristics (or exits entirely) to limit risk exposure.

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### Variable annuity market

- Financial market:
  - Asset price  $S_t$  evolves exogenously.
  - SDF that prices all assets:  $S_t = \mathbb{E}_t[M_{t,t+1}S_{t+1}]$ .
- VA issued in period t matures in period t + 2.
  - Price  $P_t$  (account value 1 plus fee  $P_t 1$ ).
  - ▶ Rollup rate *r*<sub>t</sub>.
  - ► Payoff:

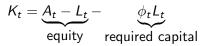
$$X_{t,t+2} = \max\left\{ (1+r_t)^2, \frac{S_{t+2}}{S_t} \right\} = \frac{S_{t+2}}{S_t} + \underbrace{\max\left\{ (1+r_t)^2 - \frac{S_{t+2}}{S_t}, 0 \right\}}_{\text{put option}}$$

- Option value:  $V_{t,t} = \mathbb{E}_t[M_{t,t+2}X_{t,t+2}].$
- ► VA is a mutual fund when r<sub>t</sub> = −1 (i.e., insurer exits the market for guarantees).

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#### Risk-based capital

Risk-based capital:



• Risk weight  $\phi_t > 0$  on liabilities.

Cost of a rating downgrade or regulatory action:

$$C_t = C(K_t)$$

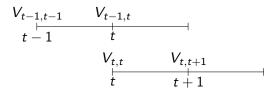
where C' < 0 and C'' > 0.

Define shadow cost of capital as

$$c_t = -\frac{\partial C_t}{\partial K_t} > 0$$

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Shocks to risk-based capital



- Adverse shock at t (i.e., lower stock prices, lower interest rates, or higher volatility).
  - 1. Value of existing liabilities  $V_{t-1,t}$  rises, lowering risk-based capital.
  - 2. Marginal cost  $V_{t,t}$  increases on new contracts.
- Shadow cost of capital  $c_t$  rises through  $V_{t-1,t-1}$ .

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## Insurer's maximization problem

• Demand:  $Q_t = Q_t(P_t, r_t)$ .

- Decreasing in price:  $\partial Q_t / \partial P_t < 0$ .
- Increasing in the rollup rate:  $\partial Q_t / \partial r_t > 0$ .
- ▶ Insurer cannot offer negative rollup rates:  $r_t \in \{-1\} \bigcup [0, \infty)$ .
- Insurer maximizes firm value:

$$\max_{P_t,r_t} (P_t - V_{t,t})Q_t - C_t.$$

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# Result 1: Optimal pricing

Optimal price is

$$P_{t} = \left(1 - \frac{1}{\epsilon_{P,t}}\right)^{-1} \underbrace{\left(V_{t,t} + \frac{c_{t}\phi_{t}(V_{t,t} - 1)}{1 + c_{t}}\right)}_{\text{marginal cost}}$$

- 1. Decreases in demand elasticity  $\epsilon_{P,t}$ .
- 2. Increases in frictionless option value  $V_{t,t}$ .
- 3. Increases in shadow cost of capital  $c_t$  and capital requirement  $\phi_t$ .
- Adverse shock increases price through
  - 1. Higher  $V_{t,t}$ .
  - 2. Higher  $c_t$  through revaluation of existing liabilities.

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## Result 2: Optimal contract characteristics

Optimal rollup rate is

$$r_{t} = \left(\frac{\partial V_{t,t}}{\partial r_{t}}\right)^{-1} \frac{\epsilon_{r,t}}{\epsilon_{P,t}-1} \left(V_{t,t} - \frac{c_{t}\phi_{t}}{1+(1+\phi_{t})c_{t}}\right) - 1 > 0$$

if interior. Otherwise, corner solution  $r_t \in \{-1, 0\}$ .

- Insurer exits the market for guarantees (i.e.,  $r_t = -1$ ) when
  - 1. Demand is inelastic to the rollup rate (i.e., low  $\epsilon_{r,t}$ ).
  - 2. Demand is price elastic (i.e., high  $\epsilon_{P,t}$ ).
  - 3. Shadow cost of capital  $c_t$  or capital requirement  $\phi_t$  is high.
- Key insight: Contract characteristics respond to risk-based capital and can lead to market incompleteness.

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# Estimation of variable annuity demand

- Decompose fee into markup vs. cost using a differentiated product demand system.
- Random-coefficients logit model implies market share for contract *i* in period *t*:

$$Q_{i,t} = \int \frac{\exp\{\alpha P_{i,t} + \beta' \mathbf{x}_{i,t} + \xi_{i,t}\}}{1 + \sum_{j=1}^{I} \exp\{\alpha P_{j,t} + \beta' \mathbf{x}_{j,t} + \xi_{j,t}\}} \ dF(\alpha,\beta).$$

- Contract characteristics: Fee, rollup rate, number of investment options, and guaranteed death benefit.
- ► Insurer characteristics: A.M. Best rating and fixed effects.
- Instruments that capture cost shocks:
  - 1. Reserve valuation: Value of existing liabilities.
  - 2. Share of reserves reinsured: Constrained insurers use reinsurance.

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# Estimated model of variable annuity demand

		Standard
Variable	Mean	deviation
Fee	-3.29	0.26
	(0.14)	(0.07)
Rollup rate	0.25	
	(0.04)	
Investment options	0.09	
	(0.01)	
Guaranteed death benefit	-5.25	
	(2.90)	
A.M. Best rating	0.73	
	(0.20)	
Observations	32,419	

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## Decomposing marginal costs

Marginal cost for contract i sold by insurer n:

$$\log(\mathsf{MC}_{i,n}-1) = \underbrace{\log(V_{i,n}-1)}_{\text{option value}} + \underbrace{\log\left(1 + \frac{c_n\phi_n}{1+c_n}\right)}_{\text{frictions}}$$

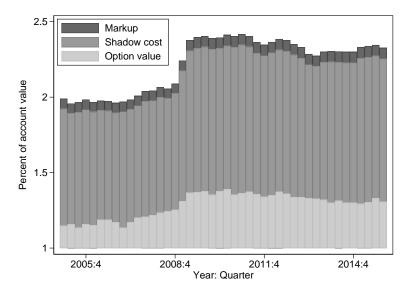
Cross-sectional regression:

$$\log(\mathsf{MC}_{i,n}-1) = \beta' \mathbf{x}_{i,n} + \nu_{i,n} + \gamma_n,$$

- x<sub>i,n</sub>: Contract characteristics (rollup rate, number of investment options, and guaranteed death benefit).
- $\gamma_n$ : Insurer fixed effects identifies shadow cost.

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# Decomposing variable annuity fees



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# Supply-side theory of insurance

	Traditional view	Supply-side view	
Products	Life/health insurance	Guaranteed return	
	& traditional annuities	products	
Insures	Idiosyncratic risk	Market risk	
	across states	across investors	
Frictions	Informational	Financial/regulatory	
	& market power		
Consequences	Variation in prices, contract characteristics		
	& degree of market incompleteness		

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Broader issues					

- Mutual funds traditionally pure pass-through institutions with no risk mismatch.
- Growing part of the mutual fund sector sold through life insurers is subject to risk mismatch.
- Similar problem to persistent under-funding of pension funds, but with additional market discipline for publicly traded companies.
- Guaranteed return products are a significant share of life insurer liabilities in Austria, Denmark, France, Germany, Netherlands, and Sweden (ESRB 2015).
- A potential issue to monitor for financial stability.