

---

# ETFs, Arbitrage, and Contagion

- ▶ **Itzhak Ben-David**

*Fisher College of Business, The Ohio State University*

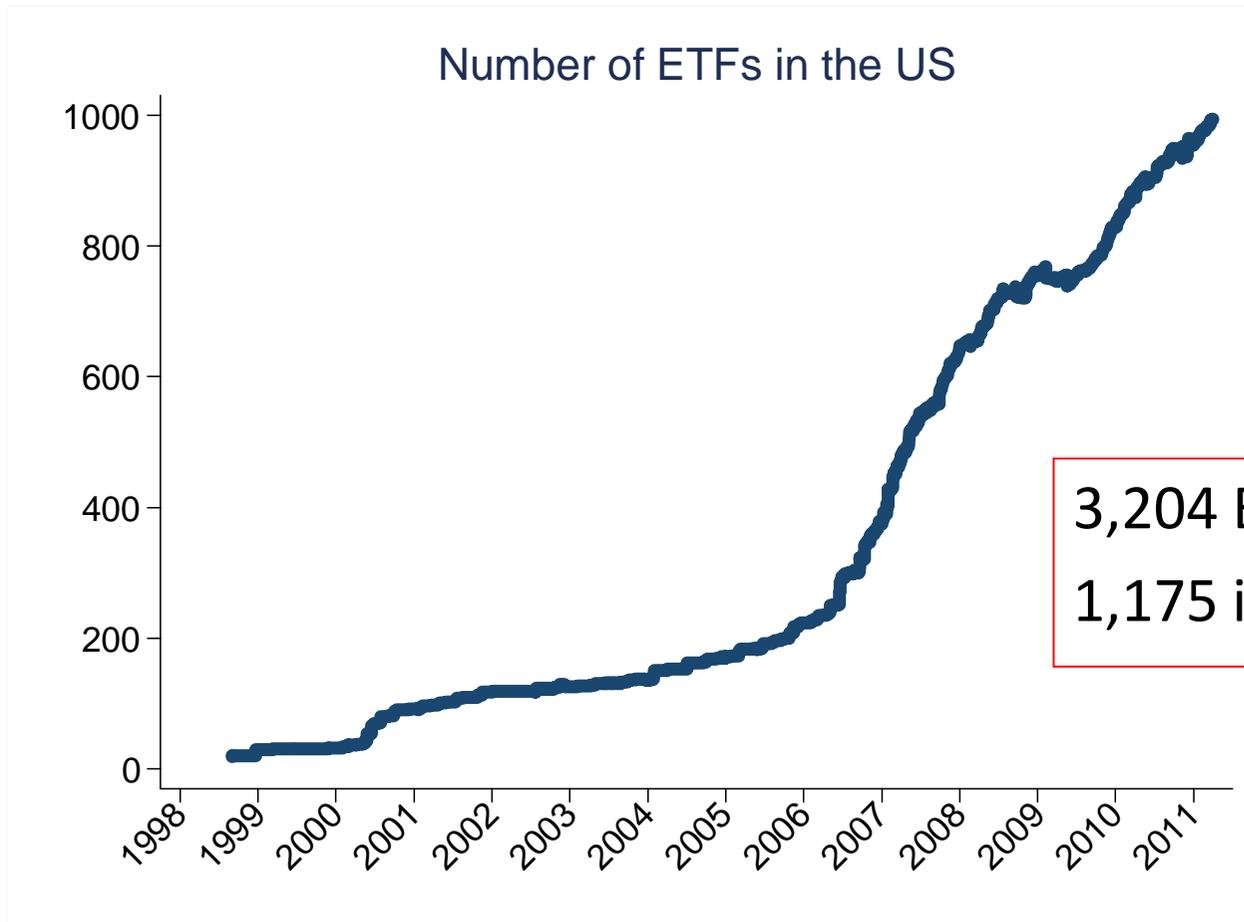
- ▶ **Francesco Franzoni**

*University of Lugano and Swiss Finance Institute*

- ▶ **Rabih Moussawi**

*Wharton Research Data Services (WRDS)*

# The Growth in the ETF Market



3,204 ETFs worldwide  
1,175 in the US

AUM in ETFs globally : \$1.5 trillion

ETF trading: up to 40% of volume in U.S. markets

## New Issues Are Raised

---

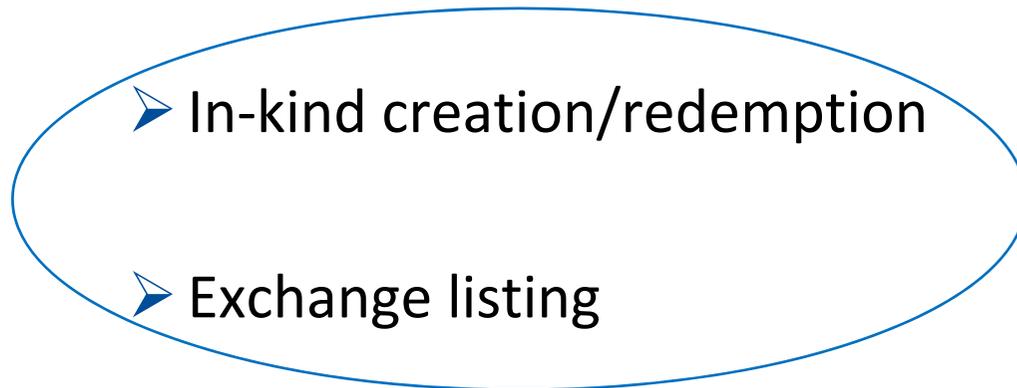
- Regulators are considering the risks from ETFs to investors and the financial system
  - Illiquidity: Flash Crash, May 6, 2010
  - Counterparty Risk
  - Systemic Risk: run on ETF assets
- Our question: Can ETFs foster contagion of liquidity shocks?

# Exchange Traded Funds (ETFs)

---

*“ETFs are investment companies that are legally classified as open-end companies or Unit Investment Trusts (UITs)” (SEC)*

- Different from standard open-end funds in:

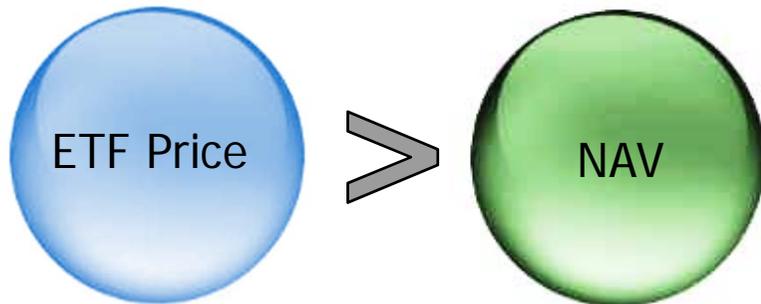


- ETF prices can deviate from NAV
- ETF prices are tied by 'arbitrage' to NAV

# ETF 'Arbitrage'

---

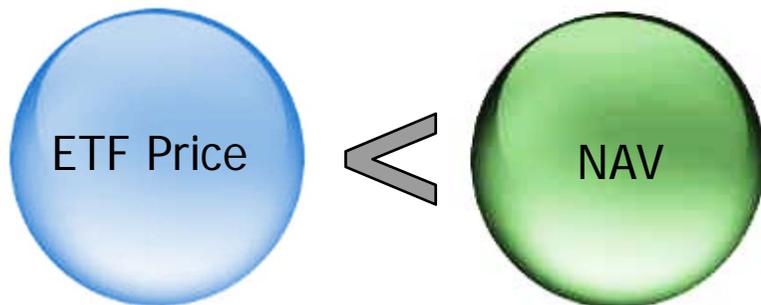
ETF Premium:



Authorized Participants:

- Buy underlying securities
- Create ETF shares in kind
- Sell ETF shares in the market

ETF Discount:



Authorized Participants:

- Buy ETF in the market
- Redeem ETF shares in kind
- Sell the underlying securities

## Other forms of ETF 'Arbitrage'

---

- Hedge funds can take long/short positions in ETF and underlying securities
  - Wait for price convergence
  - ETF replication can be optimized using a subset of underlying securities
  - High Frequency Trading
- ETF vs. Futures arbitrage

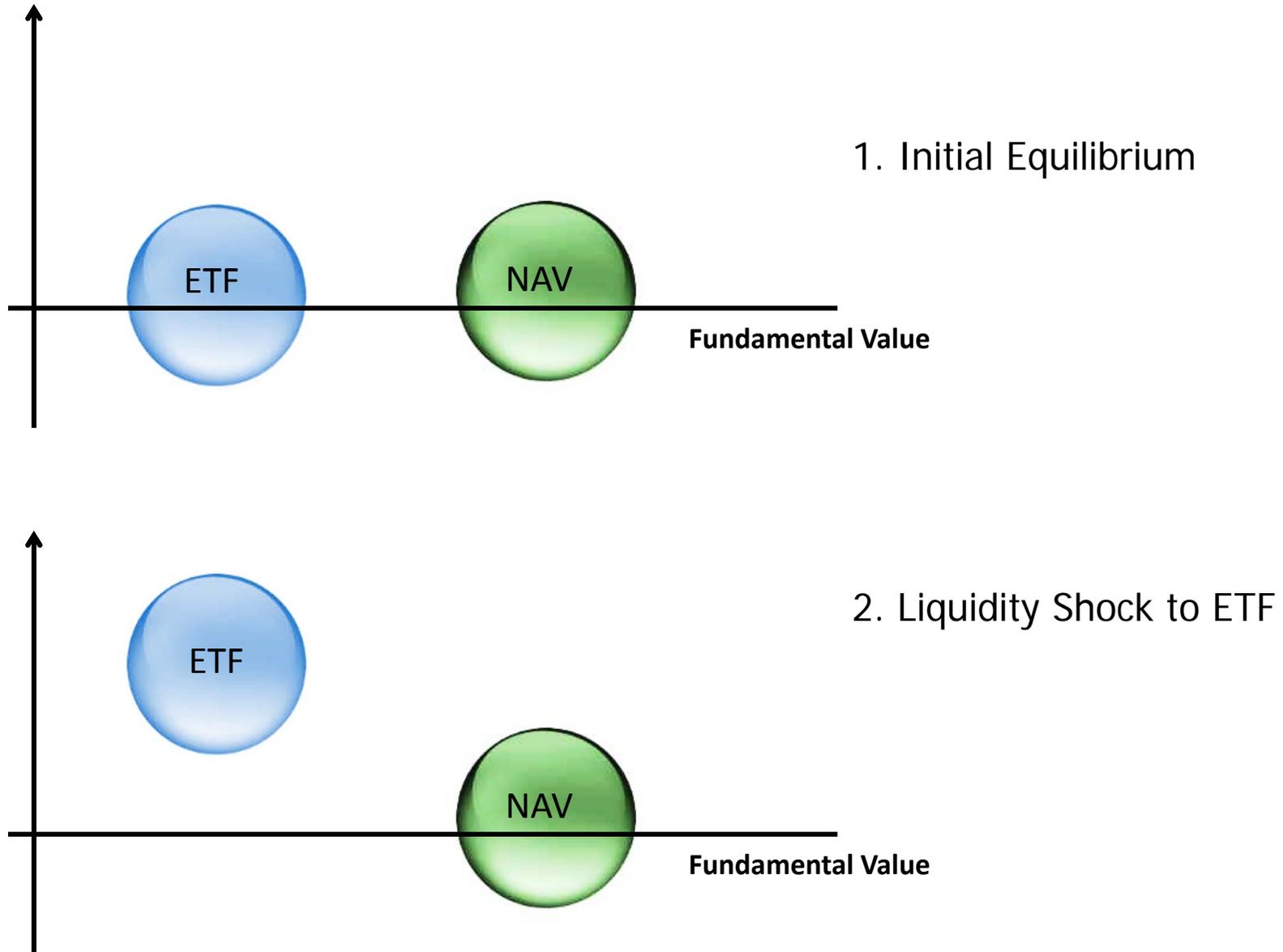
## Limited Arbitrage

---

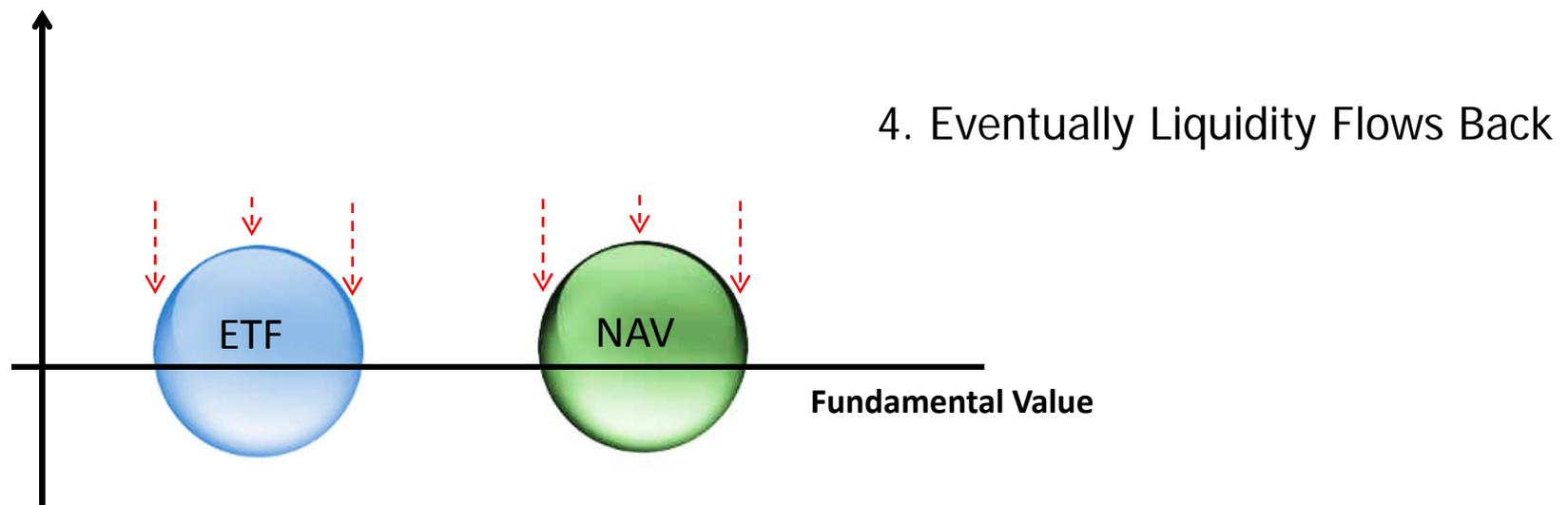
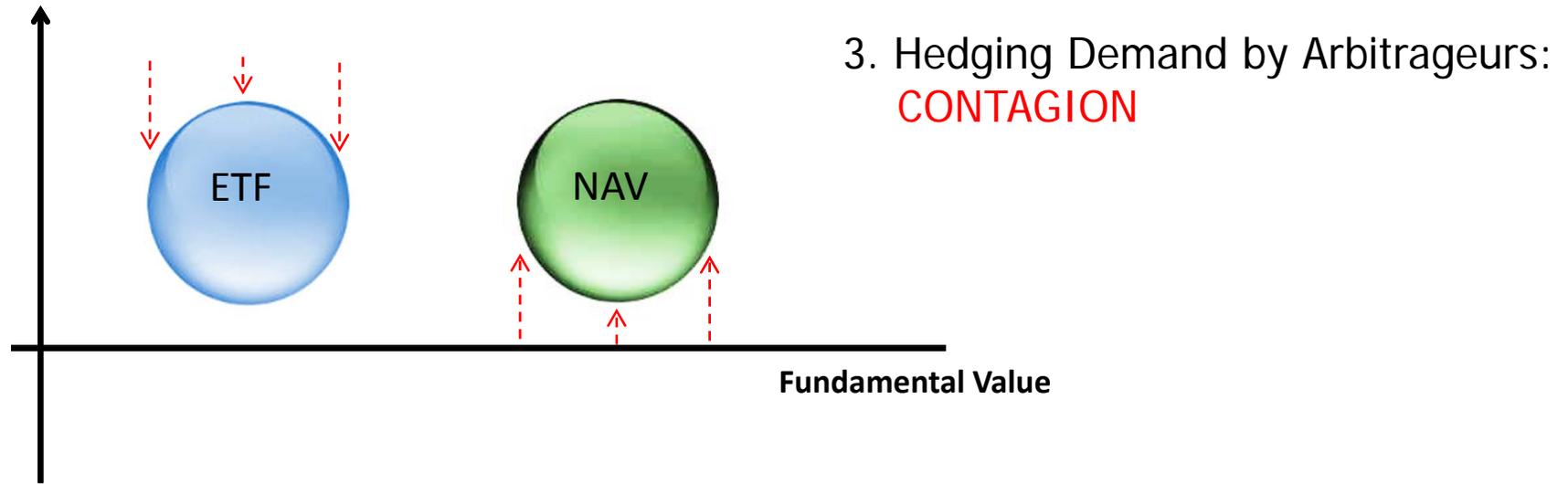
- Execution risk for APs
- Short selling costs
- Non-fundamental risk and arbitrageurs' short horizon
- Specialized arbitrageurs

# Contagion with Limited Arbitrage

---



# Contagion with Limited Arbitrage (cont'd)



# Literature

---

## ***Limits of Arbitrage***

- Shleifer and Vishny (1997), Gromb and Vayanos (2010)

## ***Contagion with Limited Arbitrage***

- Risk Averse Arbitrageurs
  - Greenwood (2005), Hau, Massa, and Peress (2010)
- Wealth Effects
  - Kyle and Xiong (2001)
- Liquidity Spillovers
  - Cespa and Foucault (2012)

## ***ETFs***

- ETF mispricing and trading strategies
  - Engle and Sarkar (2006), Marshall, Nguyen, and Visaltanachoti (2010), Petajisto (2011)
- Effects of ETF on Volatility and Liquidity
  - Trainor (2010), Bradley and Litan (2010)

# Roadmap and Results

---

1. Provide evidence of limits of arbitrage
  - Arbitrageurs' capital ↓ → Mispricing =  $(ETF - NAV)/ETF$  ↑
2. Show non-fundamental shock propagation from ETF to NAV via arbitrage
  - Mispricing (t) ↑ → NAV (t+1) ↑
  - The effect reverts within two days consistent with non-fundamental shock
  - Share creation, order imbalance, and price impacts consistent with arbitrage activity
3. Implications of shock propagation:
  - Volatility of stocks owned by ETFs ↑
  - Evidence that ETFs transmitted shocks from Futures to stock market during the Flash Crash

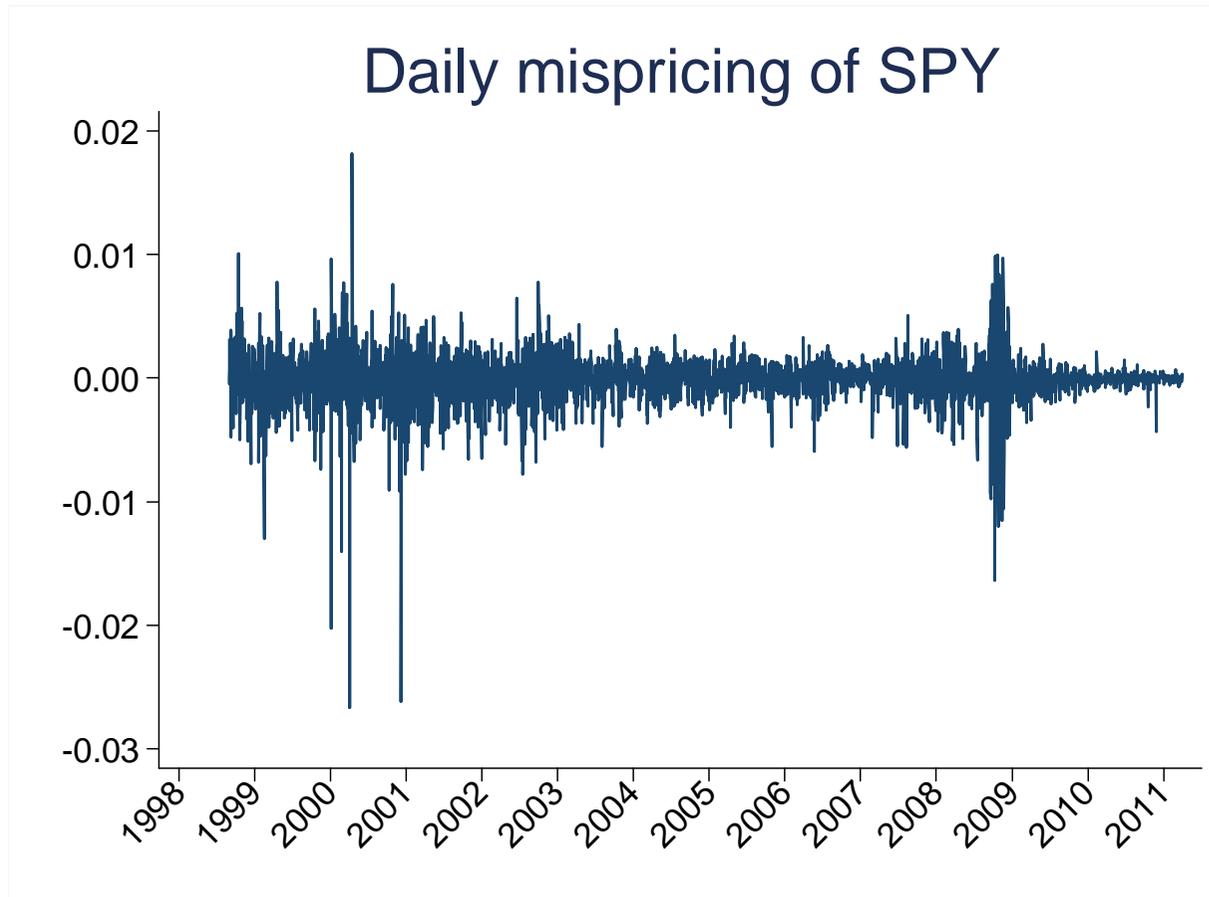
# Data

---

- **CRSP** – identify 1,261 ETFs (share code 73)
  - Returns (daily)
  - ETFs: Equity, Bonds, Commodities, Real Estate, etc.
- **Compustat** – shares outstanding (daily)
- **OptionMetrics** – shares outstanding (daily)
- **Lipper, Morningstar** – NAV (daily)
- **Thomson-Reuters Mutual Fund** – ETF holdings in stocks (quarterly)
- Period: 1998-2010
  
- Flash Crash
  - **TAQ** – Intraday analysis of Flash Crash
  - **CME** data of E-mini S&P 500 futures

# Time Series of SPY Mispricing

---



$$\text{ETF Mispricing} = (\text{ETF price} - \text{NAV}) / \text{ETF price}$$

- Large mispricing in stressed times
- Both positive and negative
- Std. Dev. of daily mispricing of SPY: 21bps

# Limits of Arbitrage (time-series)

|                                     | Dep. variable: Interquartile range of ETF mispricing |                     |                       |
|-------------------------------------|--|---------------------|-----------------------|
|                                     | Entire sample  | Excluding crisis    | Equity ETFs           |
| Past week stock market returns      | -0.009***<br>(-3.171)                                | -0.005*<br>(-1.778) | -0.012***<br>(-6.293) |
| Past week financial sector returns  | -0.003**<br>(-2.000)                                 | -0.002<br>(-1.242)  | 0.001<br>(1.268)      |
| Past week average VIX               | 0.004***<br>(5.691)                                  | 0.003***<br>(4.017) | 0.005***<br>(10.134)  |
| Past week average TED spread        | 0.031***<br>(3.227)                                  | 0.012<br>(1.170)    | 0.026***<br>(4.040)   |
| Past week average arbitrage profits | -0.037***<br>(-5.333)                                | -0.011<br>(-1.601)  | -0.016**<br>(-2.338)  |
| Observations                        | 3,098  | 2,949               | 3,098                 |
| Adj. R <sup>2</sup>                 | 0.697  | 0.700               | 0.553                 |

- Larger aggregate mispricing as a function of Limits of Arbitrage:
  - Lower returns on market and financial sector (Hameed, Kang, and Viswanathan, 2010)

# Limits of Arbitrage (time-series)

|                                     | Dep. variable: Interquartile range of ETF mispricing |                     |                       |
|-------------------------------------|--|---------------------|-----------------------|
|                                     | Entire sample  | Excluding crisis    | Equity ETFs           |
| Past week stock market returns      | -0.009***<br>(-3.171)                                | -0.005*<br>(-1.778) | -0.012***<br>(-6.293) |
| Past week financial sector returns  | -0.003**<br>(-2.000)                                 | -0.002<br>(-1.242)  | 0.001<br>(1.268)      |
| Past week average VIX               | 0.004***<br>(5.691)                                  | 0.003***<br>(4.017) | 0.005***<br>(10.134)  |
| Past week average TED spread        | 0.031***<br>(3.227)                                  | 0.012<br>(1.170)    | 0.026***<br>(4.040)   |
| Past week average arbitrage profits | -0.037***<br>(-5.333)                                | -0.011<br>(-1.601)  | -0.016**<br>(-2.338)  |
| Observations                        | 3,098  | 2,949               | 3,098                 |
| Adj. R <sup>2</sup>                 | 0.697  | 0.700               | 0.553                 |

- Larger aggregate mispricing as a function of Limits of Arbitrage:
  - VIX (Nagel, 2011)
  - TED spread (Boyson, Stahel, and Stultz, 2010)

# Limits of Arbitrage (time-series)

|                                     | Dep. variable: Interquartile range of ETF mispricing |                     |                       |
|-------------------------------------|--|---------------------|-----------------------|
|                                     | Entire sample  | Excluding crisis    | Equity ETFs           |
| Past week stock market returns      | -0.009***<br>(-3.171)                                | -0.005*<br>(-1.778) | -0.012***<br>(-6.293) |
| Past week financial sector returns  | -0.003**<br>(-2.000)                                 | -0.002<br>(-1.242)  | 0.001<br>(1.268)      |
| Past week average VIX               | 0.004***<br>(5.691)                                  | 0.003***<br>(4.017) | 0.005***<br>(10.134)  |
| Past week average TED spread        | 0.031***<br>(3.227)                                  | 0.012<br>(1.170)    | 0.026***<br>(4.040)   |
| Past week average arbitrage profits | -0.037***<br>(-5.333)                                | -0.011<br>(-1.601)  | -0.016**<br>(-2.338)  |
| Observations                        | 3,098  | 2,949               | 3,098                 |
| Adj. R <sup>2</sup>                 | 0.697  | 0.700               | 0.553                 |

- Larger aggregate mispricing as a function of Limits of Arbitrage:

➤ Lower Profits from ETF Arbitrage (Brunnermeier and Pedersen, 2009)

# Tests for contagion from ETF to NAV

---

1. Do ETF price changes predict returns on the underlying securities?
  2. Identify non-fundamental shocks
  3. Identify arbitrage trading
- Focus on US Equity ETFs (most liquid)

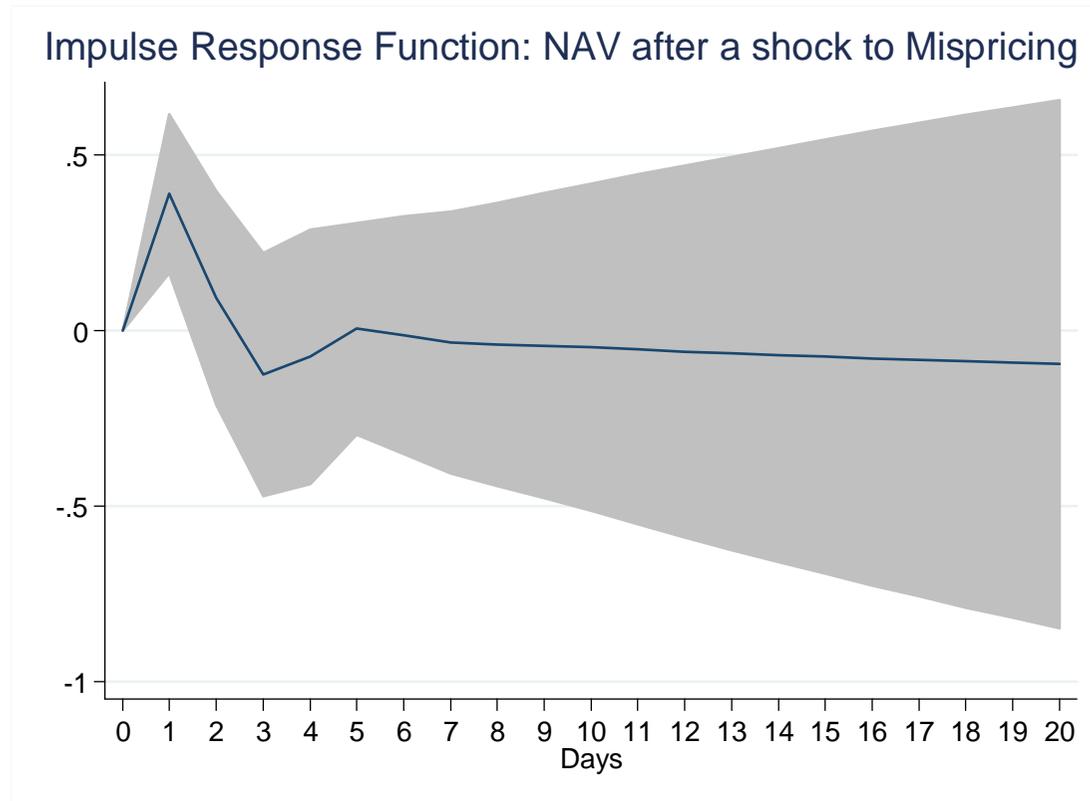
# NAV Return (t+1) Predicted by Mispricing(t) (ETF-day level sample)

|                            | NAV Ret(t+1)          |                       | ETF Ret(t+1)           |                        |
|----------------------------|-----------------------|-----------------------|------------------------|------------------------|
|                            | (1)                   | (2)                   | (3)                    | (4)                    |
| Mispricing(t)              | 0.118***<br>(10.126)  | 0.140***<br>(10.159)  | -0.316***<br>(-17.869) | -0.385***<br>(-19.006) |
| NAV Ret(t)                 | -0.071***<br>(-3.952) | -0.067***<br>(-3.803) | 0.185***<br>(6.741)    | 0.171***<br>(6.417)    |
| ETF Ret(t)                 | 0.014<br>(1.385)      | 0.010<br>(0.954)      | -0.267***<br>(-11.561) | -0.253***<br>(-11.046) |
| Calendar day fixed effects | Yes                   | Yes                   | Yes                    | Yes                    |
| ETF fixed effects          | No                    | Yes                   | No                     | Yes                    |
| Observations               | 514,797               | 514,797               | 514,835                | 514,835                |
| Adj. R <sup>2</sup>        | 0.008                 | 0.008                 | 0.068                  | 0.071                  |

- Consistent with shock propagation:
  - ETF price (liquidity shock)  $\uparrow \rightarrow$  Mispricing $>0 \rightarrow$  Arbitrage  $\rightarrow$  NAV  $\uparrow$
  - About 14% of the mispricing in  $t$  is closed by NAV change in  $t + 1$
- Controlling for NAV Ret( $t$ ):
  - Control for shocks that hit the NAV and then revert
- Larger effect of arbitrage trades is on ETF price
- Possibly: underlying stock prices are more closely tied to fundamental

## Identifying non-fundamental shocks: Reversal of NAV

---



- A shock to mispricing induces a response in the NAV that wears out in about 2 days
- Consistent with shocks to mispricing being mostly liquidity shocks that propagate to underlying securities

## Evidence of arbitrage trades: $\Delta$ ETF shares

|                            | $\Delta$ ETF Shares (t, t+1) (%) |                      |                       |                       |
|----------------------------|----------------------------------|----------------------|-----------------------|-----------------------|
|                            | (1)                              | (2)                  | (3)                   | (4)                   |
| ETF mispricing(t)          | 0.048***<br>(13.526)             | 0.041***<br>(10.780) | 0.057***<br>(15.506)  | 0.050***<br>(12.772)  |
| NAV Ret(t)                 |                                  |                      | 0.014***<br>(4.763)   | 0.012***<br>(4.429)   |
| ETF Ret(t)                 |                                  |                      | -0.017***<br>(-6.718) | -0.016***<br>(-6.431) |
| Calendar day fixed effects | Yes                              | Yes                  | Yes                   | Yes                   |
| Fund fixed effects         | No                               | Yes                  | No                    | Yes                   |
| Observations               | 514,794                          | 514,794              | 514,794               | 514,794               |
| Adj. R <sup>2</sup>        | 0.000                            | 0.006                | 0.000                 | 0.006                 |

- Shares on day  $t$  increase if mispricing increases on day  $t$ 
  - Evidence of arbitrage trades by Authorized Participants

## Evidence of arbitrage trades: Buying/Selling Pressure

| Dependent variable:             | Buy-sell order imbalance (t+1) of... |                    |
|---------------------------------|--------------------------------------|--------------------|
|                                 | ETFs                                 | Underlying Stocks  |
|                                 | (1)                                  | (2)                |
| ETF mispricing (t)              | -0.873**<br>(-2.498)                 | 0.167**<br>(2.384) |
| ETF mispricing (1-10 lags)      | Yes                                  | Yes                |
| ETF order imbalance (1-10 lags) | Yes                                  | Yes                |
| Observations                    | 365,414                              | 366,308            |
| Adj. R <sup>2</sup>             | 0.130                                | 0.030              |

- Consistent with arbitrage trading, positive mispricing predicts:
  - Negative demand pressure on ETF
  - Positive demand pressure on underlying stocks

## Evidence of arbitrage trades: Hedging Demand (S&P500)

|   | Dependent variable: Stock Return (t+1) (%) |                        |                        |                        |
|---|--|------------------------|------------------------|------------------------|
|   | (1)  | (2)                    | (3)                    | (4)                    |
| ETF mispricing (t) × log(Market capitalization) | 0.180**<br>(2.118)                         |                        |                        | 0.128<br>(1.422)       |
| log(Market capitalization)                      | -0.002***<br>(-14.689)                     |                        |                        | -0.003***<br>(-18.944) |
| ETF mispricing (t) × Beta                       |  | 0.252<br>(1.131)       |                        | 0.384*<br>(1.684)      |
| Beta  |  | -0.008***<br>(-21.028) |                        | -0.008***<br>(-18.661) |
| ETF mispricing (t) × Idiosyncratic volatility   |  |                        | -3.846<br>(-1.442)     | -6.049**<br>(-2.248)   |
| Idiosyncratic volatility                        |  |                        | -0.079***<br>(-14.823) | -0.056***<br>(-10.132) |
| Calendar day fixed effects                      | Yes  | Yes                    | Yes                    | Yes                    |
| Observations                                    | 1,250,138                                  | 1,250,385              | 1,242,366              | 1,242,366              |
| Adj. R <sup>2</sup>                             | 0.118                                      | 0.119                  | 0.119                  | 0.120                  |

- Consistent with hedging demand by arbitrageurs, effect of mispricing of S&P500 is larger on:
  - Stocks with higher weight in the index (Greenwood 2005)
  - Stocks with higher beta and lower idiosyncratic volatility (better hedges)

# Effect of $\Delta\#ETFs$ on $\Delta$ Volatility and $\Delta$ Turnover

(stock-month level sample)

|  | Monthly change in daily volatility (%) |                       | Monthly change in turnover |                       |
|--|--|-----------------------|----------------------------|-----------------------|
|  | (1)                                    | (2)                   | (3)                        | (4)                   |
| # ETFs first reporting to hold the stock | 0.016***<br>(7.455)                    | 0.019***<br>(8.286)   | 0.001***<br>(8.570)        | 0.001***<br>(8.376)   |
| # ETFs last reporting to hold the stock  | -0.038***<br>(-5.888)                  | -0.047***<br>(-6.342) | -0.003***<br>(-6.261)      | -0.003***<br>(-4.904) |
| Stock-month controls                     | Yes                                    | Yes                   | Yes                        | Yes                   |
| Calendar month fixed effects             | Yes                                    | Yes                   | Yes                        | Yes                   |
| Stock fixed effects                      | No                                     | Yes                   | No                         | Yes                   |
| Observations                             | 428,205                                | 428,205               | 424,989                    | 424,989               |
| Adj. R <sup>2</sup>                      | 0.289                                  | 0.381                 | 0.060                      | 0.075                 |
| Number of stocks                         |  | 9,269                 |                            | 9,234                 |

- More/fewer ETFs owning the stocks:
  - Higher/lower Stock Volatility
  - Higher/lower Stock Turnover

## The Flash Crash: May 6, 2010

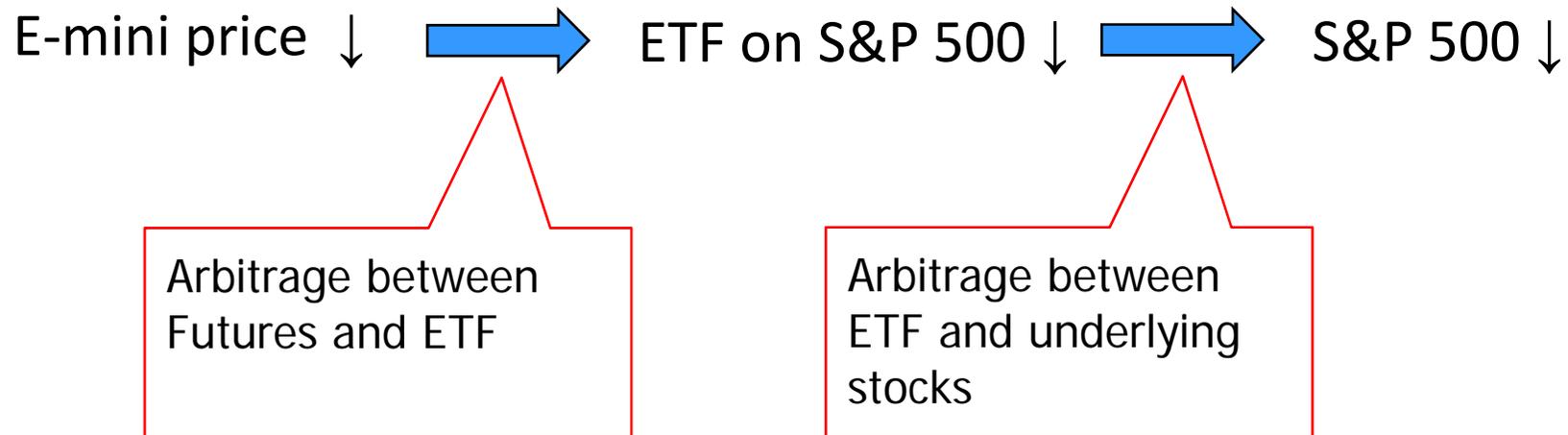
---

- The S&P 500 plunged by almost 6% in a few minutes and quickly recovered
- Some stocks fell to a few cents in value and ETFs accounted for 60% of cancelled trades
- Shock triggered by large sell order of E-mini futures (75,000 contracts) on S&P 500 by mutual fund (*Waddell and Reed*)
- How did shock propagate to stocks?

## ETFs as a channel for contagion?

---

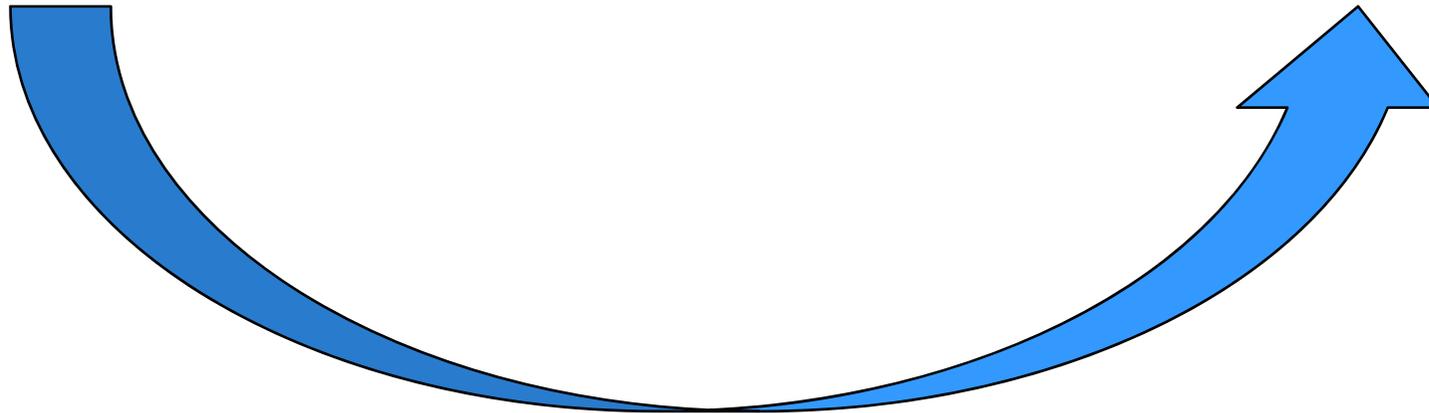
Conjecture and test that ETF arbitrage **contributed to** propagate the shock from futures to spot markets



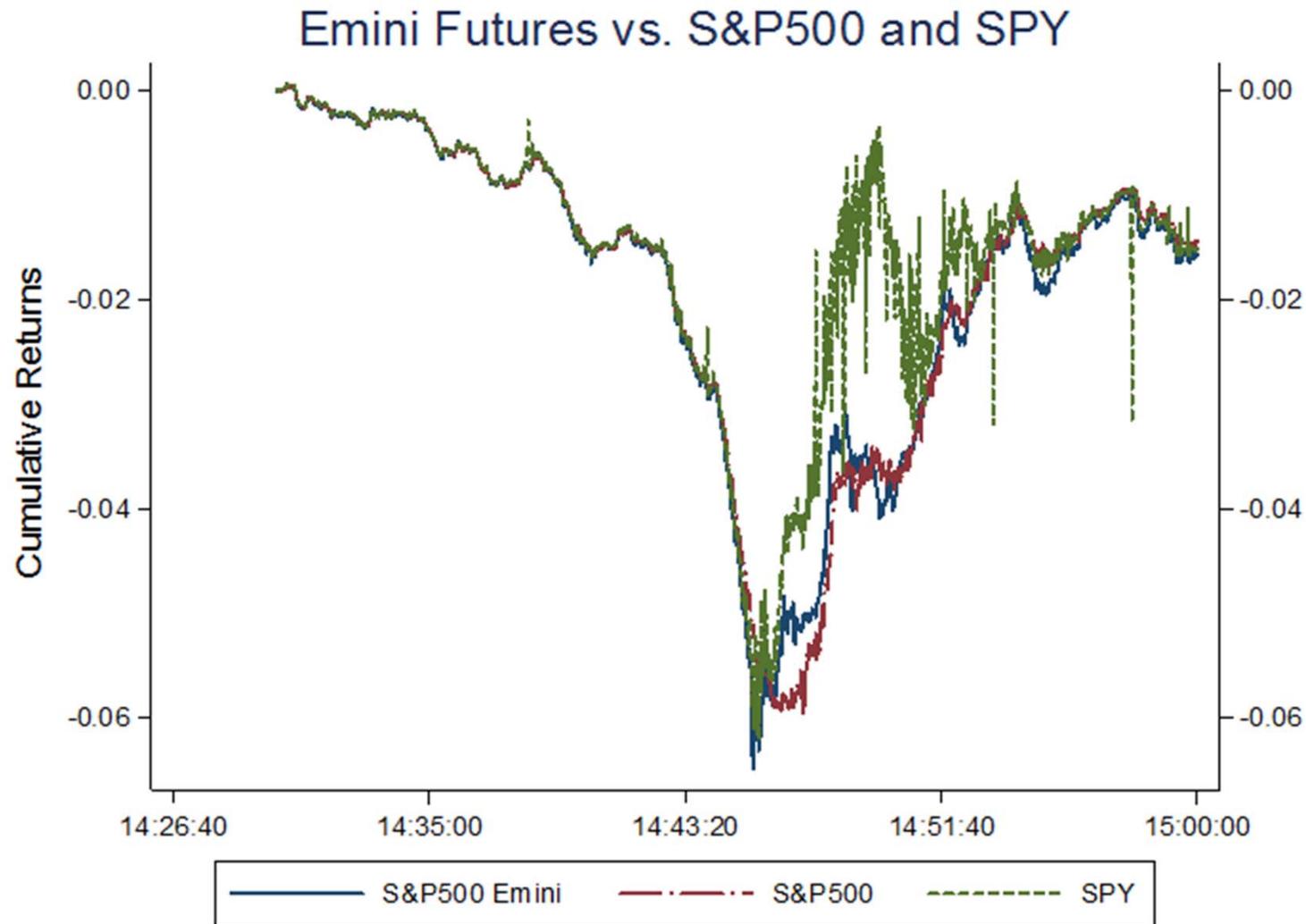
## Not the only channel, of course!

Direct arbitrage between futures and spot market  
was taking place

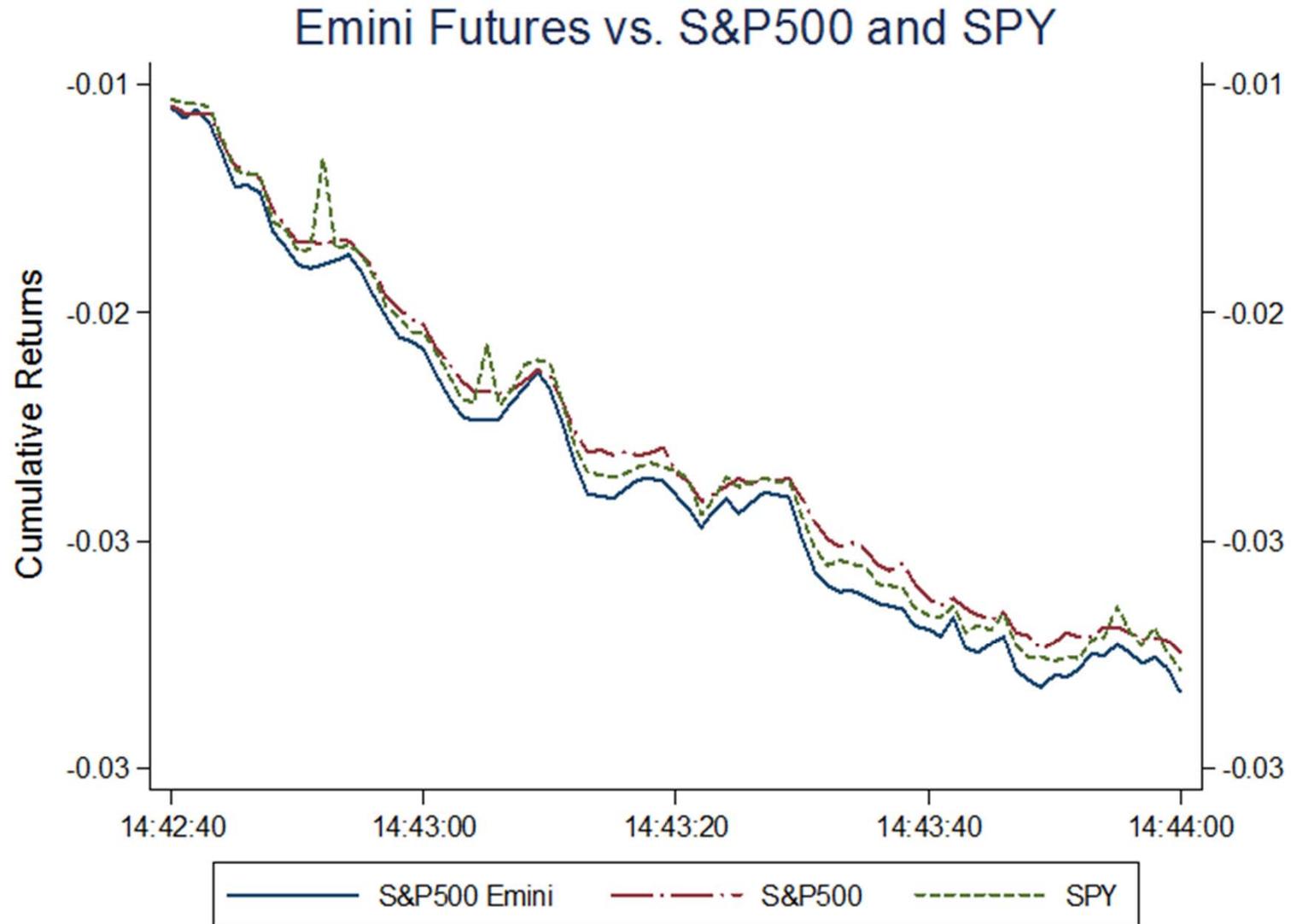
E-mini price ↓ → ETF on S&P 500 ↓ → S&P 500 ↓



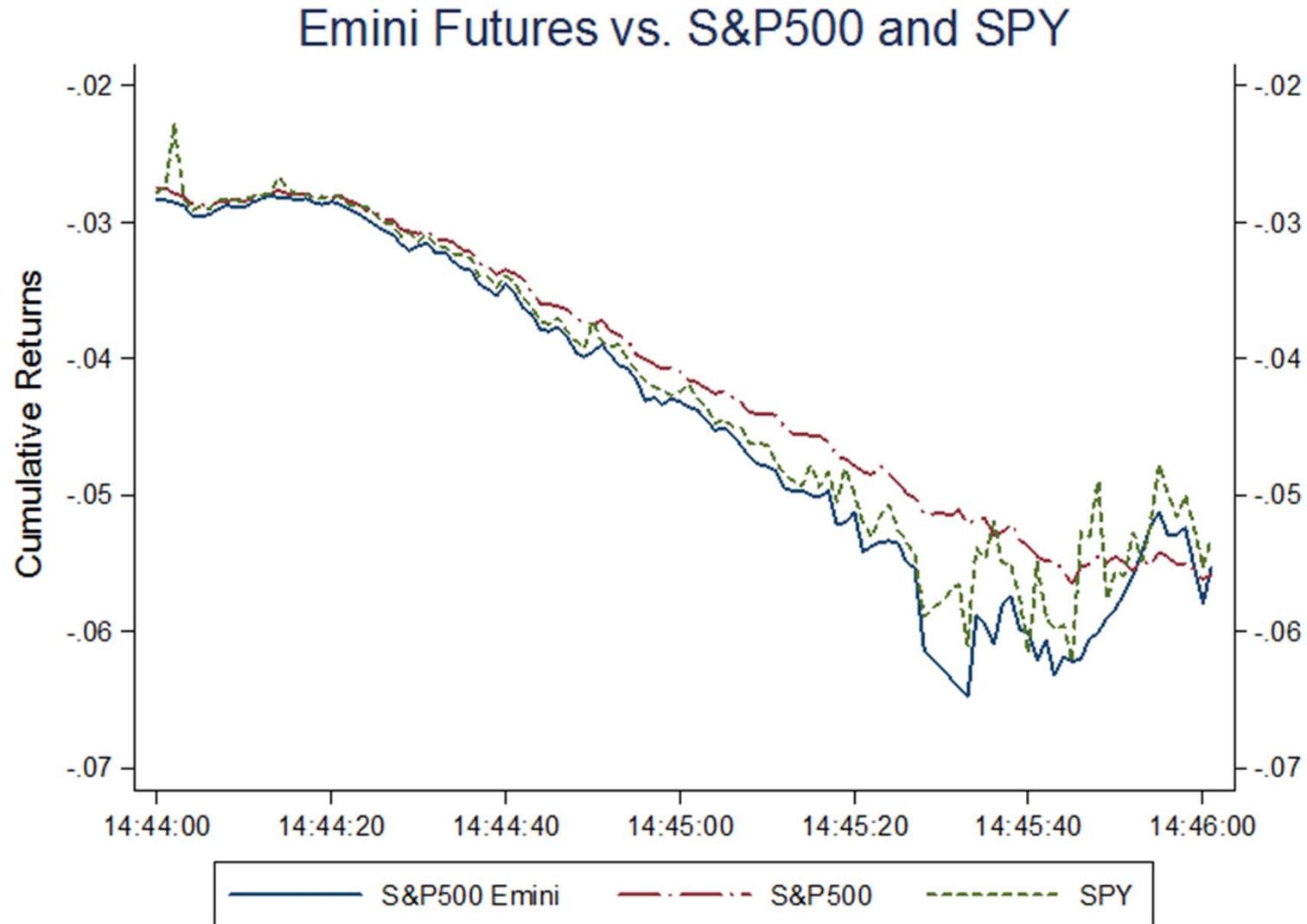
# S&P 500, E-mini, and SPY dropped together



## E-mini leads, then SPY, then S&P500 (2:42PM - 2:44PM)



## E-mini leads, then SPY, then S&P500 (2:44PM - 2:46PM)



# S&P500 Return (t+1) Predicted by SPY Mispricing(t) (second-by-second)

|                             | Dependent variable: Return S&P500 (t+1)   |                       |                       |
|-----------------------------|---|-----------------------|-----------------------|
|                             | Sample: Before trough 14:30:00 - 14:45:45 |                       |                       |
|                             | (1)                                       | (2)                   | (3)                   |
| SPY mispricing (t)          | 0.064***<br>(10.396)                      | 0.055***<br>(4.710)   | 0.025*<br>(1.812)     |
| E-mini mispricing (t)       |   |                       | 0.073***<br>(4.887)   |
| Cum. Ret. S&P500 (t, t-60)  |   | 0.082***<br>(5.516)   | 0.126***<br>(7.344)   |
| Cum. Ret. SPY (t, t-60)     |   | -0.011<br>(-0.814)    | -0.004<br>(-0.327)    |
| Cum. Ret. Emini (t, t-60)   |   | -0.058***<br>(-4.309) | -0.110***<br>(-6.813) |
| Cum. Ret. S&P500 (t, t-600) |   | -0.000<br>(-0.041)    | -0.007<br>(-1.172)    |
| Cum. Ret. SPY (t, t-600)    |   | -0.003<br>(-0.482)    | -0.002<br>(-0.349)    |
| Cum. Ret. Emini (t, t-600)  |   | 0.007<br>(1.187)      | 0.011**<br>(1.983)    |
| Observations                | 945                                       | 943                   | 937                   |
| Adj. R <sup>2</sup>         | 0.102                                     | 0.189                 | 0.223                 |

- The mispricing predicts movements in the S&P, both in the fall and the recovery
  - Controlling for non-arbitrage based stories (Cespa and Foucault, 2012)
  - Controlling for direct arbitrage between futures and S&P 500

# Conclusion

---

- We study shock propagation from ETFs to underlying securities:
  - Evidence of limits of arbitrage between ETFs and underlying securities
  - Evidence that ETF arbitrage affects prices and volatilities of underlying securities
  - Evidence that ETFs served as a conduit for contagion between the futures and the equity markets during the Flash Crash
- Results are consistent with financial innovation causing an amplification of non-fundamental volatility
- Results have implications for debate on High-Frequency Trading



# Limits of Arbitrage (cross-section)

|  | Dependent variable: abs(ETF mispricing) |                       |                      |                      |
|--|---|-----------------------|----------------------|----------------------|
|  | Sample: All ETFs                        |                       | Equity ETFs          |                      |
|  | Sample period: 1998-2010                | 2001-2010             | 1998-2010            | 2001-2010            |
|  | (1)                                     | (2)                   | (3)                  | (4)                  |
| Past week arbitrage profits              | -0.007***<br>(-4.575)                   | -0.007***<br>(-4.485) | -0.005<br>(-1.354)   | -0.005<br>(-1.403)   |
| ETF relative bid-ask spread              | 0.118***<br>(18.885)                    | 0.121***<br>(19.179)  | 0.162***<br>(15.259) | 0.162***<br>(15.658) |
| Past month return volatility             | 0.003<br>(0.618)                        | 0.003<br>(0.524)      | -0.002<br>(-0.384)   | -0.002<br>(-0.265)   |
| Past week average<br>abs(ETF mispricing) | 0.503***<br>(15.695)                    | 0.503***<br>(15.225)  | 0.453***<br>(8.366)  | 0.450***<br>(8.066)  |
| Calendar day fixed effects               | Yes                                     | Yes                   | Yes                  | Yes                  |
| ETF fixed effects                        | Yes                                     | Yes                   | Yes                  | Yes                  |
| Observations                             | 876,494                                 | 857,145               | 476,028              | 465,607              |
| Adj. R <sup>2</sup>                      | 0.459                                   | 0.462                 | 0.385                | 0.390                |

- Absolute ETF mispricing correlates with:
  - ETF-level arbitrage profits
  - ETF bid-ask spread

# NAV Return (t) Predicted by Mispricing(t-1)

(ETF-day level sample)

|                            | NAV Ret(t)           |                      |                       |                       |
|----------------------------|----------------------|----------------------|-----------------------|-----------------------|
|                            | (1)                  | (2)                  | (3)                   | (4)                   |
| Mispricing(t-1)            | 0.141***<br>(10.998) | 0.164***<br>(11.014) | 0.118***<br>(10.126)  | 0.140***<br>(10.159)  |
| NAV Ret(t-1)               |                      |                      | -0.071***<br>(-3.952) | -0.067***<br>(-3.803) |
| ETF Ret(t-1)               |                      |                      | 0.014<br>(1.385)      | 0.010<br>(0.954)      |
| Calendar day fixed effects | Yes                  | Yes                  | Yes                   | Yes                   |
| ETF fixed effects          | No                   | Yes                  | No                    | Yes                   |
| Observations               | 515,151              | 515,151              | 514,797               | 514,797               |
| Adj. R <sup>2</sup>        | 0.004                | 0.005                | 0.008                 | 0.008                 |

- Consistent with shock propagation:
  - ETF price (liquidity shock)  $\uparrow \rightarrow$  Mispricing  $> 0 \rightarrow$  Arbitrage  $\rightarrow$  NAV  $\uparrow$
  - About 14% of the mispricing in  $t - 1$  is closed by NAV change in  $t$
- Controlling for NAV Ret( $t-1$ ):
  - Control for shocks that hit the NAV and then revert

# ETF Return (t) Predicted by Mispricing(t-1)

(ETF-day level sample)

---

|                            | ETF Ret(t)             |                        |                        |                        |
|----------------------------|------------------------|------------------------|------------------------|------------------------|
|                            | (5)                    | (6)                    | (7)                    | (8)                    |
| Mispricing(t-1)            | -0.454***<br>(-27.762) | -0.539***<br>(-30.757) | -0.316***<br>(-17.869) | -0.385***<br>(-19.006) |
| NAV Ret(t-1)               |                        |                        | 0.185***<br>(6.741)    | 0.171***<br>(6.417)    |
| ETF Ret(t-1)               |                        |                        | -0.267***<br>(-11.561) | -0.253***<br>(-11.046) |
| Calendar day fixed effects | Yes                    | Yes                    | Yes                    | Yes                    |
| ETF fixed effects          | No                     | Yes                    | No                     | Yes                    |
| Observations               | 515,190                | 515,190                | 514,835                | 514,835                |
| Adj. R <sup>2</sup>        | 0.037                  | 0.044                  | 0.068                  | 0.071                  |

- Larger effect of arbitrage trades is on ETF price
- Possibly: underlying stock prices are more closely tied to fundamental

## Appendix – ETF industry

---

| Year | # ETFs | Total Mktcap (\$bn) |
|------|--------|---------------------|
| 1998 | 29     | 9                   |
| 1999 | 32     | 16                  |
| 2000 | 92     | 36                  |
| 2001 | 118    | 59                  |
| 2002 | 126    | 99                  |
| 2003 | 136    | 124                 |
| 2004 | 170    | 181                 |
| 2005 | 223    | 258                 |
| 2006 | 373    | 361                 |
| 2007 | 633    | 507                 |
| 2008 | 747    | 564                 |
| 2009 | 822    | 607                 |
| 2010 | 948    | 834                 |
| 2011 | 986    | 1'019               |

# Identifying non-fundamental shocks using buy/sell pressure (ETF-day level sample)

|   | First Stage            | Second Stage         | OLS                  |
|---|------------------------|----------------------|----------------------|
| Dependent variable:                           | Mispricing(t)          | NAV Ret(t+1)         | NAV Ret(t+1)         |
| Sample:                                       | All                    | All                  | OI ETF > 1 st dev    |
|   | (1)                    | (2)                  | (3)                  |
| Mispricing (t) (or predicted(Mispricing (t))) |                        | 0.342***<br>(3.687)  | 0.089***<br>(6.445)  |
| NAV Ret(t)                                    |                        | -0.012<br>(-0.516)   | -0.057**<br>(-2.143) |
| ETF Ret(t)                                    |                        | -0.052**<br>(-2.048) | 0.019<br>(1.264)     |
| Large positive OI in ETF                      | 0.001***<br>(17.284)   |                      |                      |
| Large negative OI in ETF                      | -0.001***<br>(-14.913) |                      |                      |
| Calendar day fixed effects                    | Yes                    | Yes                  | Yes                  |
| Observations                                  | 386,014                | 385,946              | 90,631               |
| Adj. R <sup>2</sup>                           | 0.004                  | 0.001                | 0.004                |

- Goal: identify liquidity shocks in ETF
- Single out days when order imbalance in ETF is much larger than order imbalance in Underlying Securities
  - Use large ETF order imbalance as an instrument for mispricing in IV regressions: still works!
  - Restrict sample to these days: still works!

## ETF industry

| Fund Objective Code                      | AUM (\$bn) | # Funds | VW Expense Ratio | Equity ETF |
|--|------------|---------|------------------|------------|
| S&P 500 index objective funds            | 95.6       | 4       | 0.09%            | Yes        |
| Growth funds                             | 82.6       | 94      | 0.21%            | Yes        |
| Emerging markets funds                   | 70.9       | 49      | 0.61%            | Yes        |
| Gold oriented funds                      | 57.6       | 24      | 0.44%            | No         |
| International funds                      | 53.5       | 38      | 0.35%            | Yes        |
| Small-cap funds                          | 36.7       | 30      | 0.21%            | Yes        |
| Mid-cap funds                            | 28.8       | 32      | 0.23%            | Yes        |
| Intermediate investment grade debt funds | 24.6       | 8       | 0.18%            | No         |
| Treasury inflation protected securities  | 21.2       | 5       | 0.20%            | No         |
| Dedicated short bias funds               | 20.4       | 97      | 0.94%            | No         |
| Corporate debt funds BBB-rated           | 18.7       | 8       | 0.21%            | No         |
| Growth and income funds                  | 17.9       | 19      | 0.11%            | Yes        |
| Commodities funds                        | 16.7       | 64      | 0.78%            | No         |
| Latin American funds                     | 15.0       | 13      | 0.62%            | Yes        |
| China region funds                       | 14.4       | 19      | 0.73%            | No         |
| Pacific ex Japan funds                   | 13.4       | 14      | 0.56%            | No         |
| Financial services funds                 | 13.2       | 26      | 0.40%            | Yes        |
| Natural resources funds                  | 12.3       | 25      | 0.40%            | Yes        |
| Real estate funds                        | 12.0       | 15      | 0.32%            | Yes        |
| Short investment grade debt funds        | 11.2       | 4       | 0.16%            | No         |
| Equity income funds                      | 10.3       | 13      | 0.38%            | Yes        |
| High current yield funds                 | 9.7        | 3       | 0.46%            | Yes        |
| Science & technology funds               | 9.2        | 32      | 0.37%            | Yes        |
| Short U.S. treasury funds                | 8.8        | 4       | 0.15%            | No         |
| European region funds                    | 8.2        | 25      | 0.47%            | Yes        |
| Health/biotechnology funds               | 7.6        | 22      | 0.39%            | Yes        |
| General U.S. treasury funds              | 7.5        | 14      | 0.15%            | No         |
| Basic materials funds                    | 5.9        | 19      | 0.39%            | No         |
| Currency funds                           | 5.7        | 32      | 0.47%            | No         |
| Japanese funds                           | 5.5        | 9       | 0.55%            | Yes        |
| Industrials funds                        | 5.2        | 22      | 0.37%            | Yes        |
| Ultra-short obligations funds            | 5.2        | 3       | 0.15%            | No         |
| Consumer goods funds                     | 5.0        | 15      | 0.31%            | Yes        |
| Utility funds                            | 4.8        | 16      | 0.32%            | Yes        |
| Global natural resources funds           | 4.2        | 17      | 0.55%            | Yes        |
| Diversified leverage funds               | 3.8        | 14      | 0.95%            | No         |
| Specialty/miscellaneous funds            | 3.7        | 18      | 0.56%            | No         |
| General municipal debt funds             | 3.5        | 6       | 0.24%            | No         |
| Consumer services funds                  | 3.5        | 16      | 0.34%            | Yes        |
| Global funds                             | 3.0        | 13      | 0.39%            | Yes        |
| International income funds               | 2.2        | 4       | 0.50%            | No         |
| Short municipal debt funds               | 2.0        | 6       | 0.22%            | No         |
| Emerging markets debt funds              | 2.0        | 2       | 0.57%            | No         |
| Global financial services funds          | 2.0        | 7       | 0.65%            | Yes        |
| U.S. mortgage funds                      | 1.9        | 3       | 0.25%            | No         |
| International real estate funds          | 1.6        | 7       | 0.58%            | Yes        |
| Pacific region funds                     | 1.4        | 4       | 0.16%            | No         |
| Telecommunication funds                  | 1.3        | 11      | 0.49%            | Yes        |
| International small-cap funds            | 1.0        | 3       | 0.59%            | Yes        |
| Total or Average                         | 772.3      | 948     | 0.40%            |            |

## Appendix – Summary statistics (aggregate time series)

---

### EQUITY ETFs

|   | N    | Mean    | S.D.    | Min     | Median  | Max    |
|---|------|---------|---------|---------|---------|--------|
| Daily interquartile range                           | 3104 | 0.00438 | 0.00323 | 0.00116 | 0.00348 | 0.0313 |
| Daily fraction of ETFs with positive net mispricing | 3104 | 0.298   | 0.154   | 0       | 0.322   | 0.728  |
| Past week stock market returns                      | 3099 | 0.00146 | 0.0284  | -0.186  | 0.00286 | 0.2    |
| Past week financial sector returns                  | 3099 | 0.00248 | 0.049   | -0.272  | 0.00372 | 0.373  |
| Past week average VIX                               | 3099 | 0.226   | 0.0918  | 0.1     | 0.218   | 0.729  |

| CORRELATIONS  | (1) | (2)     | (3)     | (4)     | (5)     |   |
|---|-----|---------|---------|---------|---------|---|
| Daily interquartile range                           | (1) | 1       |         |         |         |   |
| Daily fraction of ETFs with positive net mispricing | (2) | -0.3938 | 1       |         |         |   |
| Past week stock market returns                      | (3) | -0.1402 | -0.0503 | 1       |         |   |
| Past week financial sector returns                  | (4) | -0.1139 | -0.082  | 0.8849  | 1       |   |
| Past week average VIX                               | (5) | 0.6026  | -0.1866 | -0.1299 | -0.0895 | 1 |

## Appendix – Summary statistics (cross-section of ETFs)

---

|  | N      | Mean     | S.D.    | Min      | Median   | Max    |
|--|--------|----------|---------|----------|----------|--------|
| ETF Ret  | 709430 | 0.000276 | 0.018   | -0.0641  | 0.000773 | 0.0634 |
| NAV Ret  | 709430 | 0.000191 | 0.0177  | -0.0634  | 0.000704 | 0.0627 |
| abs(ETF mispricing)                                | 709430 | 0.00361  | 0.00593 | 1.52E-08 | 0.00145  | 0.0405 |
| ETF mispricing                                     | 709430 | 0.00036  | 0.00619 | -0.0274  | 0.000132 | 0.0271 |
| Past week volatility(NAV)                          | 709430 | 0.015    | 0.0123  | 0.000543 | 0.0115   | 0.0774 |
| Past week EFT return                               | 709430 | 0.00135  | 0.0376  | -0.132   | 0.00341  | 0.123  |
| ETF turnover                                       | 709430 | 0.0383   | 0.1     | 0        | 0.00914  | 0.824  |
| ETF relative bid-ask spread                        | 709430 | 0.00466  | 0.00963 | 0.000126 | 0.00182  | 0.0723 |
| Number of times ETF shares changed in past 30 days | 709430 | 3.87     | 5.68    | 0        | 1        | 25     |
| Average short interest in past 30 days             | 709430 | 0.104    | 0.234   | 0.000152 | 0.0205   | 1.46   |
| $\Delta$ ETF Shares (%)                            | 709430 | 0.142    | 1.44    | -5.17    | 0        | 10.3   |

## Appendix – Summary statistics (stock-month level)

---

|  | N      | Mean     | S.D.    | Min      | Median   | Max    |
|--|--------|----------|---------|----------|----------|--------|
| Daily volatility within the month (%)              | 545838 | 3.8      | 2.92    | 0.564    | 2.91     | 16.4   |
| Monthly change in daily volatility                 | 543456 | -0.00278 | 2.14    | -7.09    | -0.0529  | 8.28   |
| Turnover (1000x#shares traded/#shares outstanding) | 547405 | 0.292    | 2.9     | 0        | 0.0742   | 883    |
| Monthly change in turnover                         | 536522 | 30.5     | 2486    | -249058  | -0.419   | 855212 |
| ETF weight in the stock (%)                        | 421903 | 2.46     | 2.02    | 2.42E-06 | 1.87     | 9.03   |
| Monthly change in ETF weight                       | 410980 | 0.0413   | 0.278   | -0.998   | 0.000562 | 1.24   |
| Total institutional ownership (%)                  | 556285 | 43.7     | 32.5    | 0        | 41.6     | 110    |
| Monthly change in institutional ownership          | 545740 | 0.177    | 2.56    | -10.1    | 0        | 12.5   |
| # ETFs first reporting to hold the stock           | 421903 | 0.54     | 1.58    | 0        | 0        | 21     |
| # ETFs last reporting to hold the stock            | 421903 | 0.113    | 0.405   | 0        | 0        | 7      |
| # ETFs reporting to hold the stock                 | 421903 | 14.2     | 13.7    | 1        | 11       | 87     |
| log(market capitalization/1000)                    | 547405 | 19.4     | 2.12    | 11.7     | 19.3     | 27.1   |
| Interquintile mispricing of ETFs in the month      | 559469 | 0.00455  | 0.00288 | 0.00159  | 0.0036   | 0.0163 |
| log(volume)  | 547526 | 16.8     | 2.41    | 3        | 17       | 25.4   |

# Appendix – Summary statistics (Flash Crash)

---

## WHOLE SAMPLE

|                                   | N    | Mean      | S.D.     | Min      | Median     | Max     |
|-----------------------------------|------|-----------|----------|----------|------------|---------|
| Return S&P500                     | 1800 | -8.13E-06 | 0.000467 | -0.00368 | -0.0000138 | 0.00355 |
| SPY mispricing                    | 1800 | 0.00342   | 0.00772  | -0.00951 | 0.000141   | 0.0324  |
| Return Emini                      | 1794 | -6.78E-06 | 0.00051  | -0.00641 | -0.0000152 | 0.00627 |
| Return SPY                        | 1800 | -8.52E-06 | 0.00242  | -0.025   | -0.0000167 | 0.0251  |
| S&P500 Order Imbalance            | 1801 | -0.0123   | 0.0497   | -0.34    | -0.0059    | 0.251   |
| SPY average short volume (t, t+5) | 1801 | 0.0016    | 0.00143  | 0.000013 | 0.00117    | 0.011   |

## BEFORE TROUGH

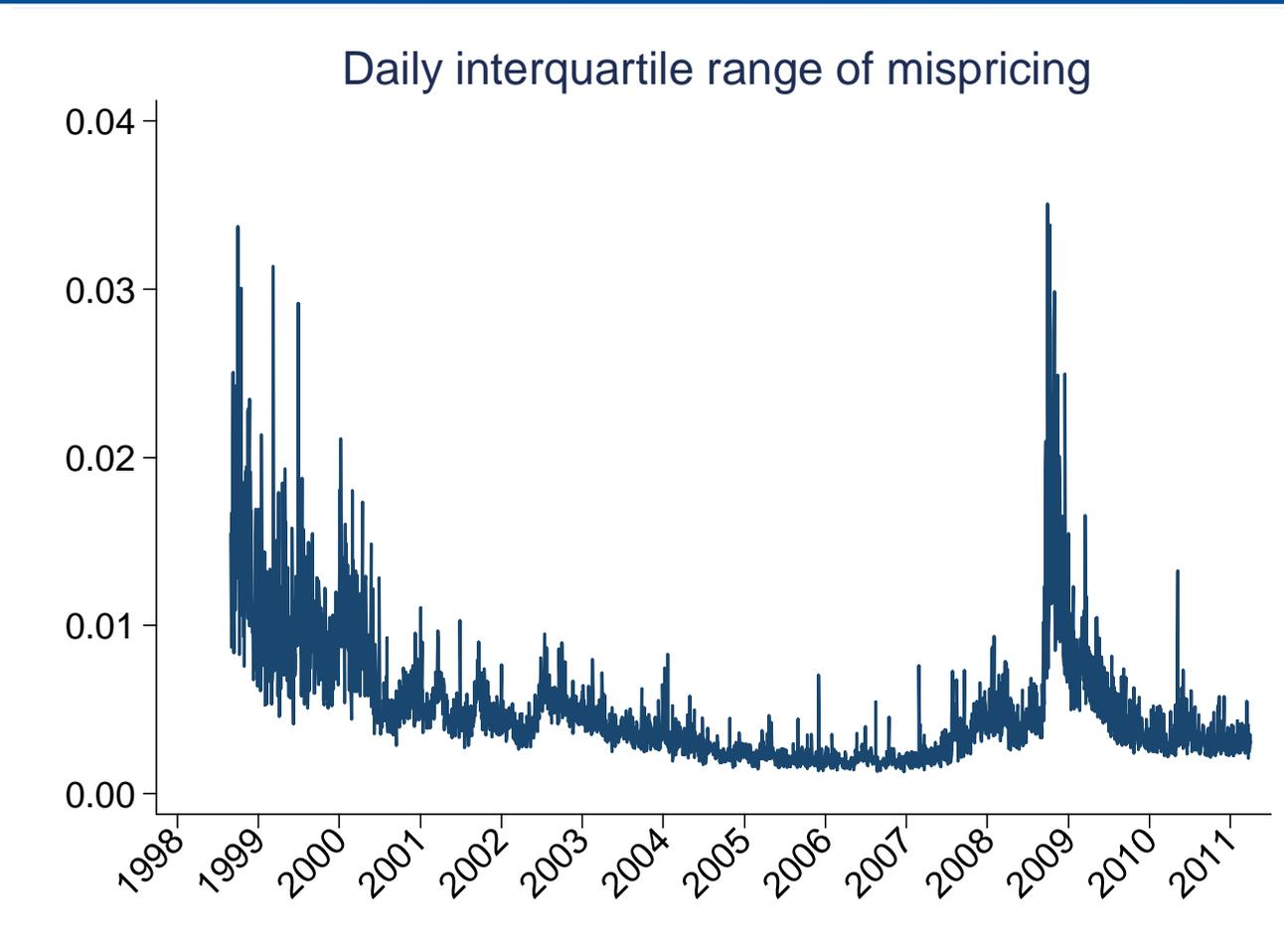
|                                   | N   | Mean       | S.D.     | Min      | Median     | Max      |
|-----------------------------------|-----|------------|----------|----------|------------|----------|
| Return S&P500                     | 945 | -0.0000616 | 0.000209 | -0.00136 | -0.0000234 | 0.000713 |
| SPY mispricing                    | 945 | -0.000132  | 0.00104  | -0.00951 | 0.0000801  | 0.00526  |
| Return Emini                      | 939 | -6.45E-05  | 0.000453 | -0.00641 | -0.0000316 | 0.00627  |
| Return SPY                        | 945 | -0.0000679 | 0.000683 | -0.00559 | -0.0000307 | 0.00762  |
| S&P500 Order Imbalance            | 946 | -2.31E-02  | 0.0579   | -0.34    | -0.0152    | 0.251    |
| SPY average short volume (t, t+5) | 946 | 0.00148    | 0.00118  | 0.000013 | 0.00117    | 0.00916  |

## AFTER TROUGH

|                                   | N   | Mean      | S.D.     | Min       | Median    | Max     |
|-----------------------------------|-----|-----------|----------|-----------|-----------|---------|
| Return S&P500                     | 855 | 0.0000509 | 0.000636 | -0.00368  | 0.0000393 | 0.00355 |
| SPY mispricing                    | 855 | 0.00735   | 0.00975  | -0.00605  | 0.00214   | 0.0324  |
| Return Emini                      | 855 | 0.0000566 | 0.000559 | -0.00301  | 0.0000201 | 0.00298 |
| Return SPY                        | 855 | 0.0000571 | 0.00344  | -0.025    | 0.0000257 | 0.0251  |
| S&P500 Order Imbalance            | 855 | -0.000281 | 0.0348   | -0.223    | 0.00287   | 0.14    |
| SPY average short volume (t, t+5) | 855 | 0.00175   | 0.00166  | 0.0000158 | 0.00115   | 0.011   |

# Time Series of all ETFs Mispricing

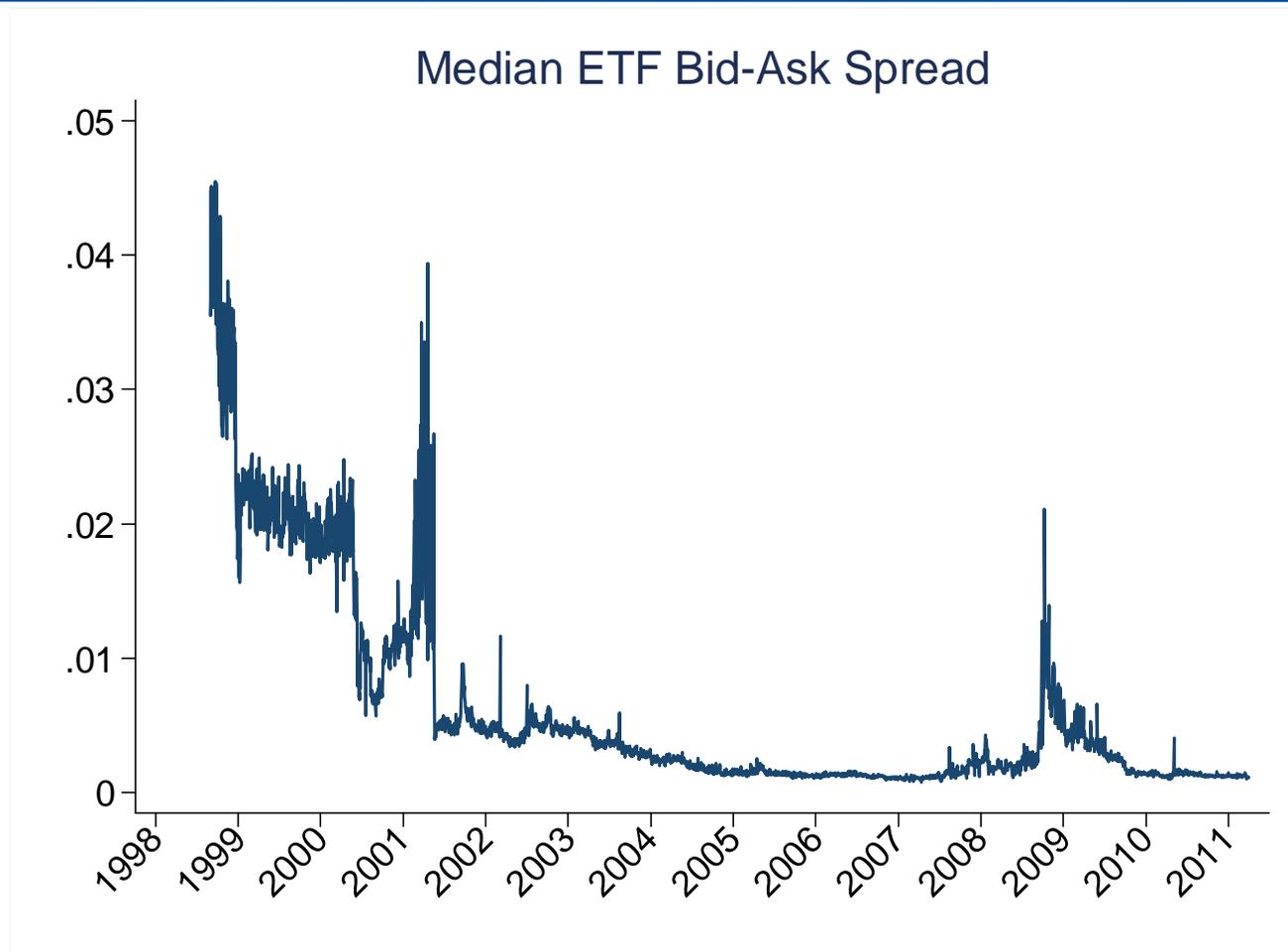
---



- Initial illiquidity of ETFs
- Mispricing increases in stressed markets

# Time Series of ETF bid-ask spread

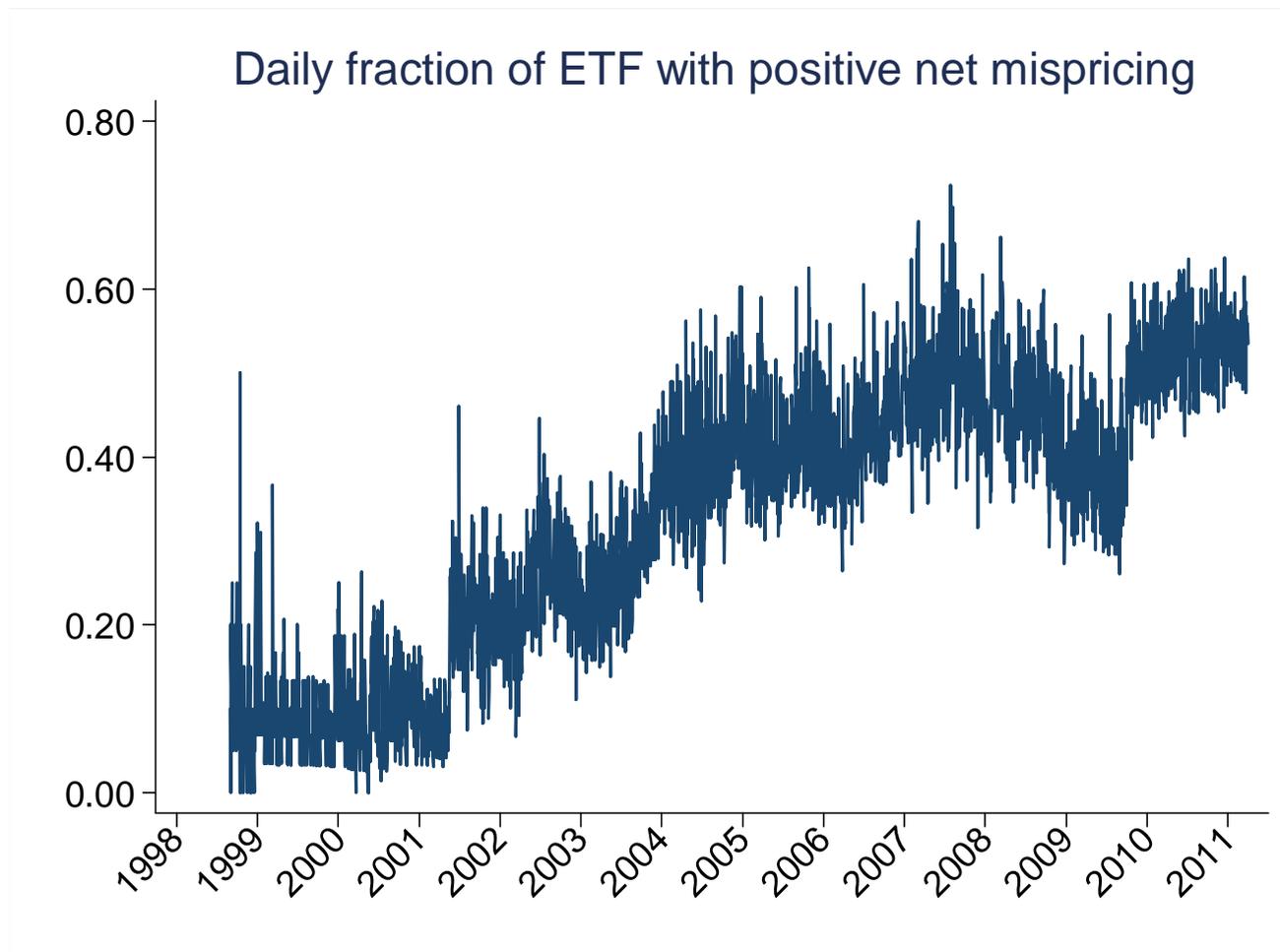
---



- Initial illiquidity of ETFs
- Bid-Ask spread increases in stressed markets

# Time Series of ETF Net Mispricing

---



- Net mispricing =  $|\text{ETF mispricing}| - \text{ETF Bid-Ask Spread}$
- During crisis, more ETFs with mispricing that exceeds bid-ask spread

# Effect of $\Delta$ ETF ownership on $\Delta$ Volatility

(stock-month level sample)

|   | Change in volatility |          |          |          |
|---|----------------------|----------|----------|----------|
| I(small stock) $\times$ Change in ETF weight              |                      |          | 0.088*** | 0.088*** |
|   |                      |          | (4.160)  | (4.128)  |
| Change in ETF weight                                      | 0.030**              | 0.031*** | -0.012   | -0.011   |
|   | (2.556)              | (2.618)  | (-0.946) | (-0.876) |
| I(small stock)  |                      |          | 0.012*** | 0.029*** |
|   |                      |          | (2.733)  | (3.161)  |
| Change in institutional ownership                         | 0.008***             | 0.008*** | 0.007*** | 0.007*** |
|   | (6.555)              | (6.818)  | (5.535)  | (5.475)  |
| I(small stock) $\times$ Change in institutional ownership |                      |          | 0.001    | 0.002    |
|   |                      |          | (0.394)  | (0.793)  |
| Stock fixed effects                                       | No                   | Yes      | No       | Yes      |
| Calendar day fixed effects                                | Yes                  | Yes      | Yes      | Yes      |
| Observations  | 431,807              | 431,807  | 431,792  | 431,792  |
| Adj. R <sup>2</sup>                                       | 0.101                | 0.102    | 0.101    | 0.102    |
| Number of stocks  |                      | 9,279    |          | 9,279    |

- 1% increase in the ETF weight raises daily volatility by 3 bps
- For the median stock in Dec 2010 (4.3% ETF ownership), volatility increased by 13 bps (3.4% of daily volatility)
- For stock in 90<sup>th</sup> pctl in Dec 2010 (7.9% ETF ownership), volatility increased by 24 bps (6.3% of daily volatility)

# Effect of new S&P500-ETFs introduction on volatility

(stock-month level sample)

| Sample: 2 months around            | Dependent variable: Daily volatility (%) |                        |                        |                        |                       |                       |
|------------------------------------|--|------------------------|------------------------|------------------------|-----------------------|-----------------------|
|                                    | introduction of IVV                      |                        |                        | introduction of VOO    |                       |                       |
|                                    | (1)                                      | (2)                    | (3)                    | (4)                    | (5)                   | (6)                   |
| Post introduction × Stock in index | 0.571***<br>(6.955)                      | 0.475***<br>(6.090)    | 0.427***<br>(5.757)    | 0.176***<br>(3.305)    | 0.183***<br>(3.689)   | 0.227***<br>(5.120)   |
| Post introduction                  | -1.464***<br>(-36.036)                   | -1.365***<br>(-36.000) | -1.408***<br>(-37.876) | -0.404***<br>(-11.872) | -0.250***<br>(-7.622) | -0.398***<br>(-7.395) |
| Stock in index                     | -2.566***<br>(-24.854)                   | -1.897***<br>(-15.168) |                        | -1.407***<br>(-28.588) | 0.157**<br>(2.143)    |                       |
| Month fixed effects                | No                                       | Yes                    | Yes                    | No                     | Yes                   | Yes                   |
| Stock fixed effects                | No                                       | No                     | Yes                    | No                     | No                    | Yes                   |
| Observations                       | 13,127                                   | 13,092                 | 13,092                 | 8,004                  | 7,973                 | 7,973                 |
| Adj. R <sup>2</sup>                | 0.069                                    | 0.324                  | 0.301                  | 0.061                  | 0.352                 | 0.255                 |
| Number of stocks                   |  |                        | 6,687                  |                        |                       | 4,029                 |

- Two new S&P500 ETFs: iShares (May, 2000) and Vanguard (Sep, 2010)
- Arguably: exogenous event relative to stock volatility
- Volatility went up for stocks in the S&P 500 in the month after the introduction of the two ETFs:
  - 50 bps increase in daily volatility after iShares
  - 20 bps increase in daily volatility after Vanguard

# ETF ownership, Volatility, and Limits of Arbitrage

(stock-month level sample)

|  | Daily volatility in month t |                        |                        |                        |
|--|-----------------------------|------------------------|------------------------|------------------------|
| Avg interquartile mispricing × ETF weight              | -9.297***<br>(-7.136)       | -12.016***<br>(-9.683) | -3.803***<br>(-2.621)  | -9.053***<br>(-6.520)  |
| Avg interquartile mispricing × Institutional ownership |                             |                        | -0.933***<br>(-10.579) | -0.463***<br>(-5.111)  |
| ETF weight   | -0.135***<br>(-20.008)      | -0.014<br>(-1.598)     | -0.080***<br>(-10.672) | 0.010<br>(1.148)       |
| Institutional ownership                                |                             |                        | -0.009***<br>(-16.418) | -0.010***<br>(-13.383) |
| log(market capitalization)                             | -1.092***<br>(-72.330)      | -1.061***<br>(-67.173) | -1.033***<br>(-68.584) | -0.992***<br>(-60.154) |
| log(volume)  | 0.771***<br>(59.082)        | 0.944***<br>(88.594)   | 0.813***<br>(63.724)   | 0.967***<br>(89.997)   |
| Stock fixed effects                                    | No                          | Yes                    | No                     | Yes                    |
| Calendar day fixed effects                             | Yes                         | Yes                    | Yes                    | Yes                    |
| Observations   | 639,547                     | 639,547                | 639,411                | 639,411                |
| Adj. R <sup>2</sup>                                    | 0.481                       | 0.396                  | 0.492                  | 0.400                  |
| Number of permnos                                      |                             | 9,081                  |                        | 9,081                  |

- The impact of ETF ownership on stock volatility is smaller at times when limits of arbitrage are stronger
  - Controlling for ownership by all institutions

# Preview of Results: Limits of Arbitrage

---

Limits of Arbitrage  
(liquidity, volatility,  
arbitrageurs' capital, etc.)



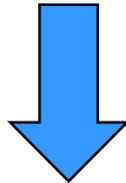
ETF mispricing  
(ETF price – NAV)

Limits of Arbitrage in ETFs

# Preview of Results: Effect on Returns

---

ETF mispricing  $\uparrow$



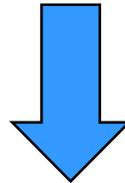
Next-day NAV  $\uparrow$

Shock to ETF price  
propagated to NAV

# Preview of Results: Effect on Volatility

---

ETF stock ownership ↑



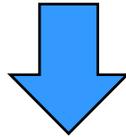
Stock volatility ↑

ETFs increase volatility of  
underlying stocks

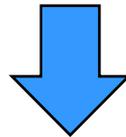
# Preview of Results: Flash Crash

---

Shock S&P500 futures



Mispricing SPDR ETF



Change in S&P 500

ETFs operate as a conduit for  
shock propagation