

# Intermediated Asymmetric Information, Compensation and Career Prospects.

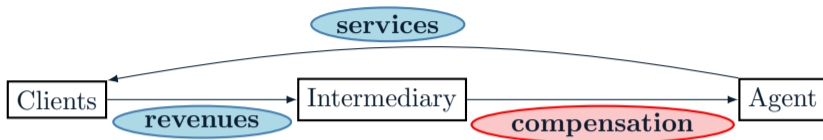
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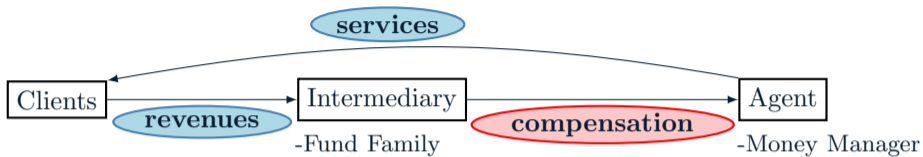
13<sup>th</sup> conference of the Paul Woolley Centre  
in collaboration with the Bank of International Settlements

# Employment Intermediation



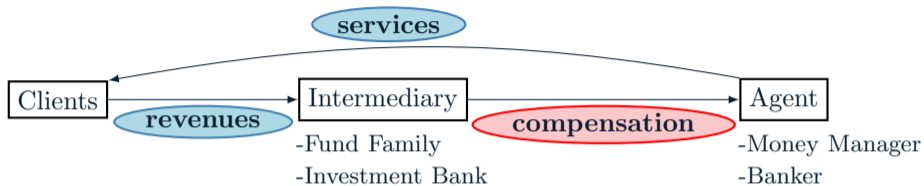
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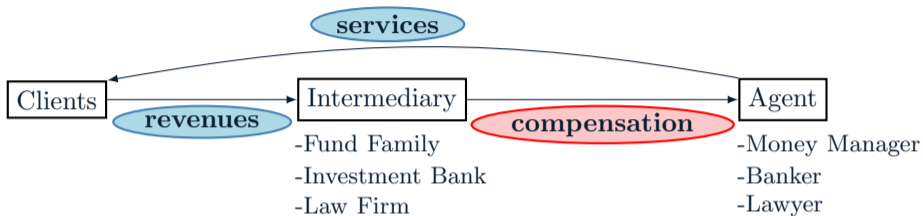
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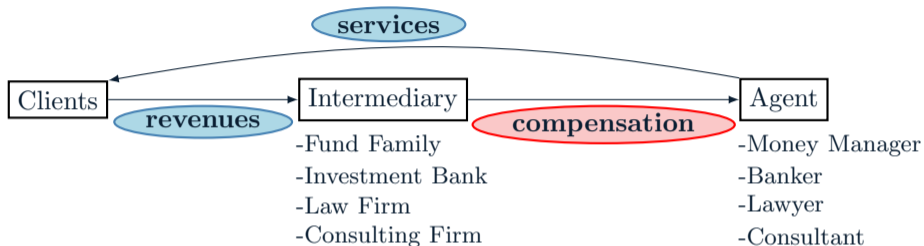
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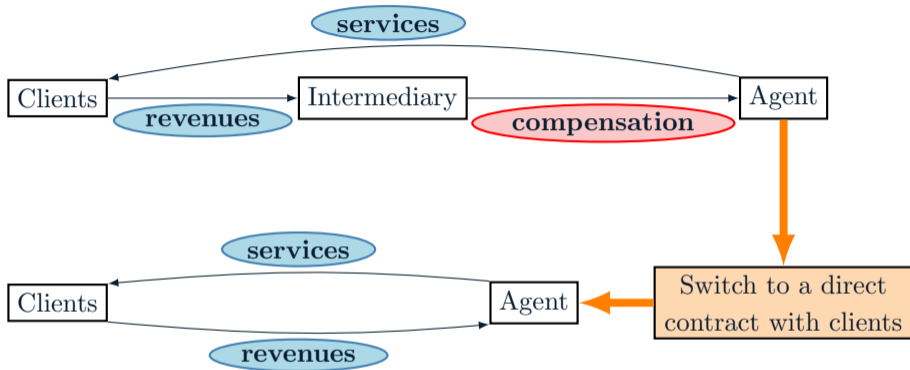
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- ▶ Labor intermediation is common in professions where skill is important.
- ▶ All parties learn about ability from the quality of past services.
  - But the intermediary knows more about the agent than the clients.
- ▶ Limited transparency:
  - clients do not observe agent's compensation but do observe if agent is retained

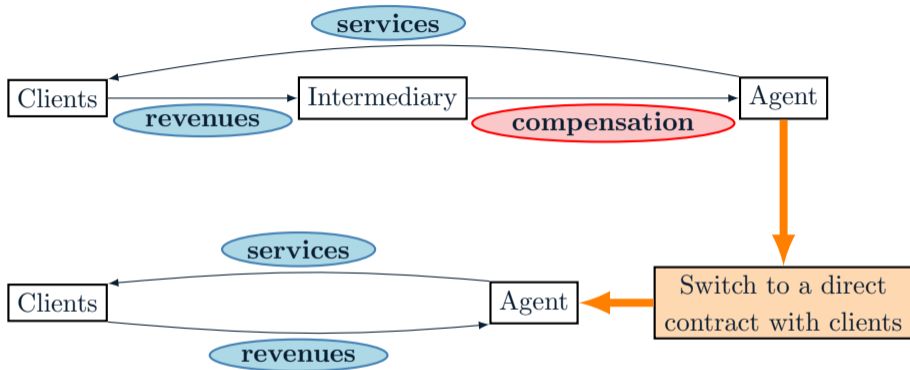
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  - Implication of lateral moves is similar.
- ▶ Intermediary benefits from high revenues and low compensation costs.

# Intermediary's Advantage in Identifying Talent

- ▶ Key idea: **the agent is let go because he develops too strong of a bargaining stance with the intermediary over compensation**, not because he is unskilled.
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- ▶ High asymmetric information: the intermediary can expropriate the agent's talent.
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  - This profit wedge declines as information asymmetry reduces asymmetric information.
- ▶ Low asymmetric information: **the intermediary speeds up information revelation** by churning lower skilled agents.
  - This is profitable - **high skilled agents pay for reputation** building.
  - Even though asymmetric information is reduced even faster.

## Related Literature From Many Fields

- ▶ **Finance Labor Market:** Berk, van Binsbergen, and Liu (2017), Deuskar, Pollet, Wang, and Zheng (2011), Strobl and Van Wesep (2012), Gao, Wang, and Yu (2019).
- ▶ **Labor Markets with Frictions:** Greenwald (1986), Farber and Gibbons (1996), Acemoglu and Pischke (1998), Chevalier and Ellison (1999), Postel-Vinay and Robin (2002), Tervio (2009).
- ▶ **Adverse Selection:** Spence (1973), Noldeke and Van Damme (1990), Fuchs and Skrzypacz (2010), Daley and Green (2012), Fuchs, Green, Papanikolaou (2016).
- ▶ **Career Concerns:** Berk and Green (2004), Holmström (1999), Board and Meyer-ter-Vehn (2013).

# Players and Setup

- ▶ **Intermediary** employs at most one agent at any given time.
  - **knows more about the agent's ability than clients;**
  - sets compensation  $\tilde{w}_t$  privately;
  - lets the agent go at an observable time  $\tau$ ;
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- ▶ **Clients'** demand for services is increasing in their perception of agent's quality

$$\text{Firm Revenue} = \mathbf{A}(\mathbb{E}_t[\theta]).$$

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$$r_I = \mu - f - \lambda(1 - \mathbf{E}_t[\theta]) - g(\mathbf{AUM}_t),$$

$$\Rightarrow \mathbf{AUM}_t = g^{-1}(\mu - f - \lambda - r_I + \lambda \cdot \mathbf{E}_t[\theta]).$$

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- ▶ Intermediary's revenue is

$$\mathbf{A}(\mathbf{E}_t[\theta]) \stackrel{def}{=} f \cdot g^{-1}(\mu - f - \lambda - r_I + \lambda \cdot \mathbf{E}_t[\theta]).$$

# Performance and Private Information in the Poisson Model

- ▶ When agent is hired, intermediary and agent observe a private signal about  $\theta$ .
  - Identify agent's type with his private belief about  $\theta$ , denoted by  $\tilde{p}_0 \sim F(\cdot)$ .
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- ▶ Publicly observable performance signals follow a negative Poisson process for tractability:

$$X_t \stackrel{def}{=} \mu dt - dN_t^\theta.$$

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- ▶ Intermediary and agent also learn from performance signals

$$\tilde{p}_t \stackrel{def}{=} \frac{\tilde{p}_0}{\tilde{p}_0 + (1 - \tilde{p}_0)e^{-\lambda t}} \cdot \mathbb{1}\{X_t = \mu t\}.$$

- ▶ Clients do not observe  $\tilde{p}_t$ , but learn from performance and retention.

# Value of Opening Own Firm

- ▶ Clients' belief about the agent who opens his own firm at time  $t$  is

$$k_t \stackrel{def}{=} P_t(\theta = 1 | \tau = t)$$

- In equilibrium,  $k_t$  is the lowest type of agent still employed on path.
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- ▶ Agent's expected value of opening own firm if his belief is  $\tilde{p}_t$  but clients' belief is  $k_t$  is

$$U(\tilde{p}_t, k_t) \stackrel{def}{=} \max_{\hat{\eta}} E_{\tilde{p}_t} \left[ \int_t^{\hat{\eta}} e^{-\rho(s-t)} A \left( \frac{k_t}{k_t + (1 - k_t)e^{-\lambda(s-t)}} \right) ds + e^{-\rho(\hat{\eta}-t)} L \right]$$

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- ▶ Clients' belief about agents who are retained by the intermediary

$$q_t \stackrel{def}{=} P_t(\theta = 1 | \tau > t, X_t) = E[\tilde{p}_t | \tilde{p}_t > k_t] \stackrel{def}{=} Q(k_t, t).$$

- Adverse selection implies a wedge  $q_t = Q(k_t, t) > k_t$ .

# Equilibrium Definition

The equilibrium is a stopping time  $\tau$ , type-specific private wage process  $(\tilde{w}_t)_{t \geq 0}$ , and processes  $(q_t)_{t \geq 0}$  and  $(k_t)_{t \geq 0}$  such that

(i) **Optimality:**  $\tau$  and  $\tilde{w}$  are optimal for the intermediary

$$(\tau, \tilde{w}) \in \arg \max_{\hat{\tau}, \hat{w}} \mathbb{E}_{\tilde{p}_0} \left[ \int_0^{\hat{\tau}} e^{-rt} (A(q_t) - \hat{w}_t) dt + e^{-r\tau} \cdot \mathbf{V} \right]$$

subject to the retention constraint in every history

$$\mathbb{E}_t \left[ \int_t^\tau e^{-\rho(s-t)} \hat{w}_s ds + e^{-\rho(\tau-s)} \cdot U(\tilde{p}_\tau, k_\tau) \right] \geq U(\tilde{p}_t, k_t).$$

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(iii) **Belief Consistency:** belief processes  $(k_t, q_t)_{t \geq 0}$  are consistent with  $\tau$ .

## High Profit Wedge: $A(q_t) - A(k_t) > r \cdot V$

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- ▶ Retaining all agents is optimal if profit wedge is sufficiently high

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- ▶ Performance gradually reveals agent's skill and reduces intermediary's advantage.
  - Mathematically, the worst agent belief  $k_t$  gets closer to  $q_t = Q(k_t, t)$ .
  - **Even as revenue  $A(q_t)$  grows, the intermediary's profit wedge shrinks.**



# Churning and Pay for Reputation

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- ▶ Being retained increases perceived skill of lowest remaining agent by  $\gamma_t dt$ :

$$\dot{k}_t = \underbrace{\lambda k_t(1 - k_t)}_{\text{learning from performance}} + \underbrace{\gamma(k_t, t)}_{\text{learning from churning}}$$

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- ▶ Retained agents value reputation increases and are willing to pay for it:

$$w(\tilde{p}_t, k_t) = \underbrace{A(k_t)}_{\text{reservation wage}} - \underbrace{\gamma(k_t, t) \cdot \partial_2 U(\tilde{p}_t, k_t)}_{\text{pay for reputation}}$$

- Selective retention by the intermediary is a signal of ability to the market: **higher skilled workers are willing to pay for it.**

# Agent's Single-Crossing

## Proposition:

*An agent with a higher private belief about his skill is more sensitive to changes in clients' beliefs:*

$$\partial_2 U(\tilde{p}', k) > \partial_2 U(\tilde{p}, k) \quad \forall \tilde{p}' > \tilde{p}.$$

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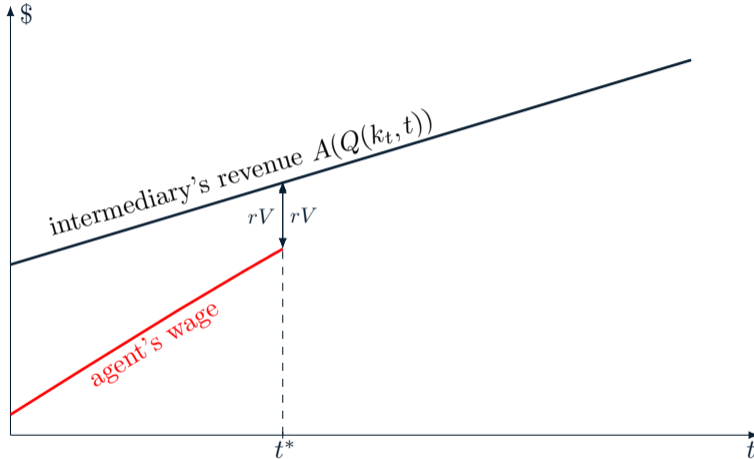
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- ▶ Churning rate is determined by the profitability of the worst remaining agent

$$rV = A(Q(k_\tau, \tau)) - w(k_\tau, k_\tau) \quad \Rightarrow \quad \gamma(k_\tau, \tau) = \frac{rV + A(k_\tau) - A(Q(k_\tau, \tau))}{\partial_2 U(k_\tau, k_\tau)} > 0.$$

- ▶ In many cases the churning set  $\mathbb{T} = [t^*, t]$ .

# Compensation Dynamics



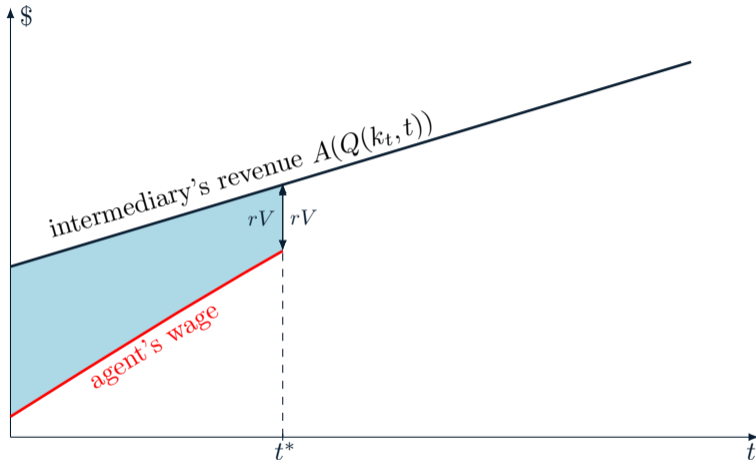
- ▶ While uncertainty is high, all agents are paid the same wage.



# Compensation Dynamics

- ▶ Better agents are retained for longer but pay more for building reputation.

# Intermediary's Profitability across Agents



- ▶ Intermediary's profit initially declines with uncertainty.

# Intermediary's Profitability across Agents

- ▶ As she begins to churn lower skilled agents, higher skilled agents pay for reputation.
- ▶ **Profits are non-monotone with respect to information asymmetry.**

# Firm Value Fixed Point

- ▶ Intermediary's equilibrium value  $V$  determines her incentives to replace an agent.
  - $V$  is the solution to a fixed point

$$\mathbf{V} = e^{-r\Delta} \cdot \mathbb{E} \left[ \int_0^\tau e^{-rt} (A(q_t) - \tilde{w}_t) dt + e^{-r\tau} \cdot \mathbf{V} \right] - I$$

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  - And how persistent it is.

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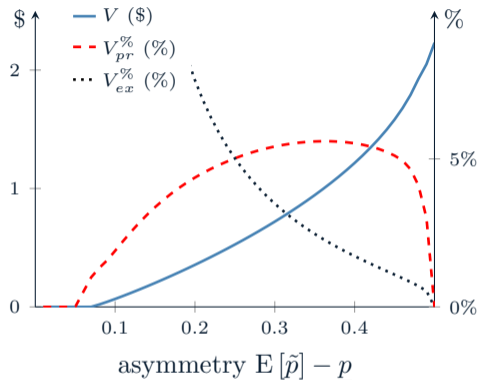
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  - And how persistent it is.
- ▶ Intermediary's profits come from expropriation and pay-for-reputation.
  - Percent of profits resulting from the agents paying for reputation:

$$V_{pr}^{\%} \stackrel{\text{def}}{=} \frac{\mathbb{E} \left[ \int_0^\tau e^{-rt} (A(\mathbf{k}_t) - \tilde{w}_t) dt \right]}{\mathbb{E} \left[ \int_0^\tau e^{-rt} (A(\mathbf{Q}(\mathbf{k}_t, t)) - \tilde{w}_t) dt \right]}.$$

# Value given Stock of Private Information

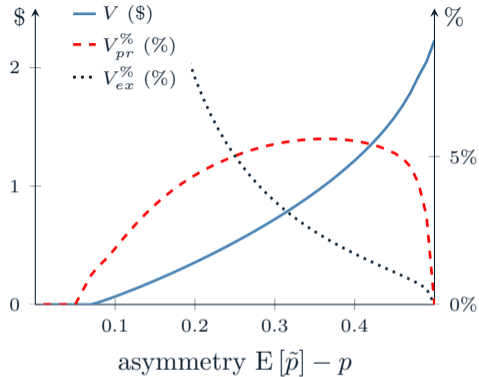


**Figure 1:** Equilibrium value  $V$  and percentage of revenues obtained from pay-for-reputation.

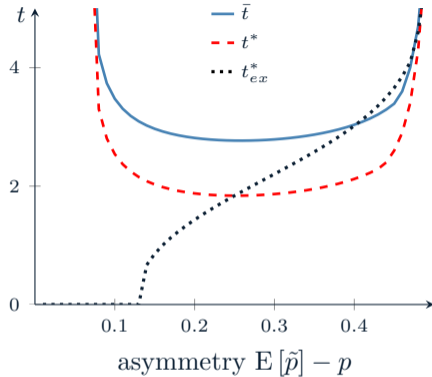
► Low asymmetry  $\Rightarrow$  a new agent is not that profitable  $\Rightarrow t^* \uparrow, V_{pr}^{\%} \downarrow$ .



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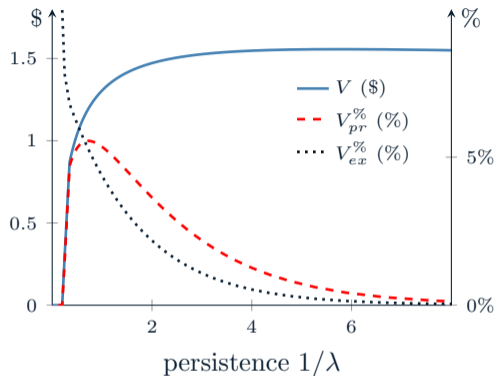
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**Figure 2:** Churning start and end times.

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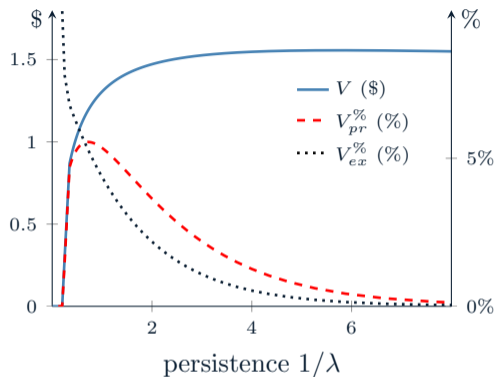
# Value given Persistence of Private Information



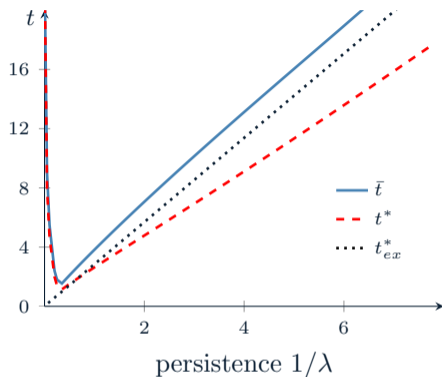
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- ▶ **Pay-for-reputation dynamics hold.** And some additional insights:
  1. Multiple churning regions where churning happens after recent bad performance.
  2. Profit wedge/asymmetric information is increasing in performance.
  3. Agents who survive a “crisis” are better compensated going forward.
  4. Three-dimensional equilibrium dynamics, change-of-measure and parallel computing to obtain comparative statics.

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  - Efficiency can increase in intermediary's profits as it improves capital allocation.